

New determination of period and quality factor of Chandler wobble, considering geophysical excitations*

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Outline:

- ◆ Introduction;
- ◆ Description of the data;
- ◆ New method proposed;
- ◆ Results based on 40-year data series;
- ◆ Conclusions.

**Based on paper submitted to Advances in Space Research*

Introduction:

- ◆ Excitations by geophysical fluids play dominant role in polar motion. Rapid changes of amplitude & phase of the free term (Chandler wobble) occur near the epochs of geomagnetic jerks (GMJ), as recently demonstrated by:
 - ◆ **Gibert & le Mouél (2008), or**
 - ◆ **Vondrák & Ron (2015), who demonstrated that better agreement with observations is obtained if additional impulse-like excitations due to GMJ are added to the effects of geophysical fluids.**
- ◆ Here we propose a new method of determining period and Q -factor of Chandler wobble, using the numerical integration of broad-band Liouville equations with these geophysical excitations.

Data used (1974.0-2014.0), all of them smoothed and long-periodic part removed:

◆ **Polar motion, as observed by different techniques (optical astrometry before 1988, space geodesy afterwards):**

◆ **IERS C04 combined solution;**

◆ **Geophysical fluids:**

◆ **Atmospheric excitations: ERA, with 6-hour steps;**

◆ **Oceanic excitations: OMCT, with 6-hour steps;**

◆ **Geomagnetic jerks (rapid changes of geomagnetic field):**

◆ **Epochs 1978.0, 1986.0, 1991.0, 1994.0, 1999.0, 2003.5, 2004.7, 2007.5, 2011.0.**

Method of determining period P and Q -factor

- ◆ We use numerical integration of Brzezinski's broadband Liouville equations with geophysical excitations, in two variants:
 - ◆ Atmospheric + oceanic excitations only;
 - ◆ Atmospheric, oceanic + GMJ excitations,
- ◆ for three different intervals:
 - ◆ 1974.0-1994.0,
 - ◆ 1994.0-2014.0,
 - ◆ 1974.0-2014.0.
- ◆ The integration is repeated for many different combinations of P , Q ; for each combination the best fitting initial pole position (and amplitudes of GMJ excitations) is found.
- ◆ P , Q values yielding the best root-mean-square (rms) fit to observed pole path are then chosen.

Brzeziński's broad-band Liouville equations (in complex form):

$$\begin{aligned} \ddot{p} - i(\sigma_C + \sigma_f)\dot{p} - \sigma_C\sigma_f p = \\ = -\sigma_C \left\{ \sigma_f(\chi_p + \chi_w) + \sigma_C(a_p\chi_p + a_w\chi_w) + i[(1+a_p)\dot{\chi}_p + (1+a_w)\dot{\chi}_w] \right\} \end{aligned}$$

where

p is the polar motion;

σ_C, σ_f are Chandler and Free Core Nutation frequency;

χ_p, χ_w , are pressure and wind term of the excitation;

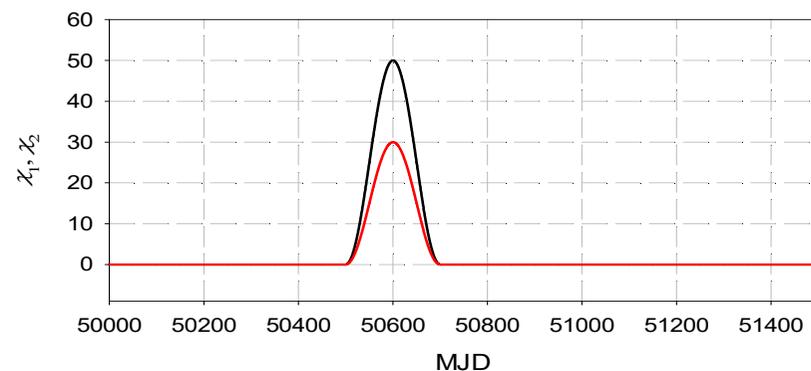
$a_p = 9.200 \times 10^{-2}$, $a_w = 2.628 \times 10^{-4}$ are numerical constants.

We fix the value of $\sigma_f = -6.31498 + 0.000153i$ [rad/day], and calculate $\sigma_C = \Omega(1+i/2Q)/P$, where $\Omega = 6.30038$ rad/day is the mean speed of Earth's rotation.

Numerical integration of Brzeziński's eqs.:

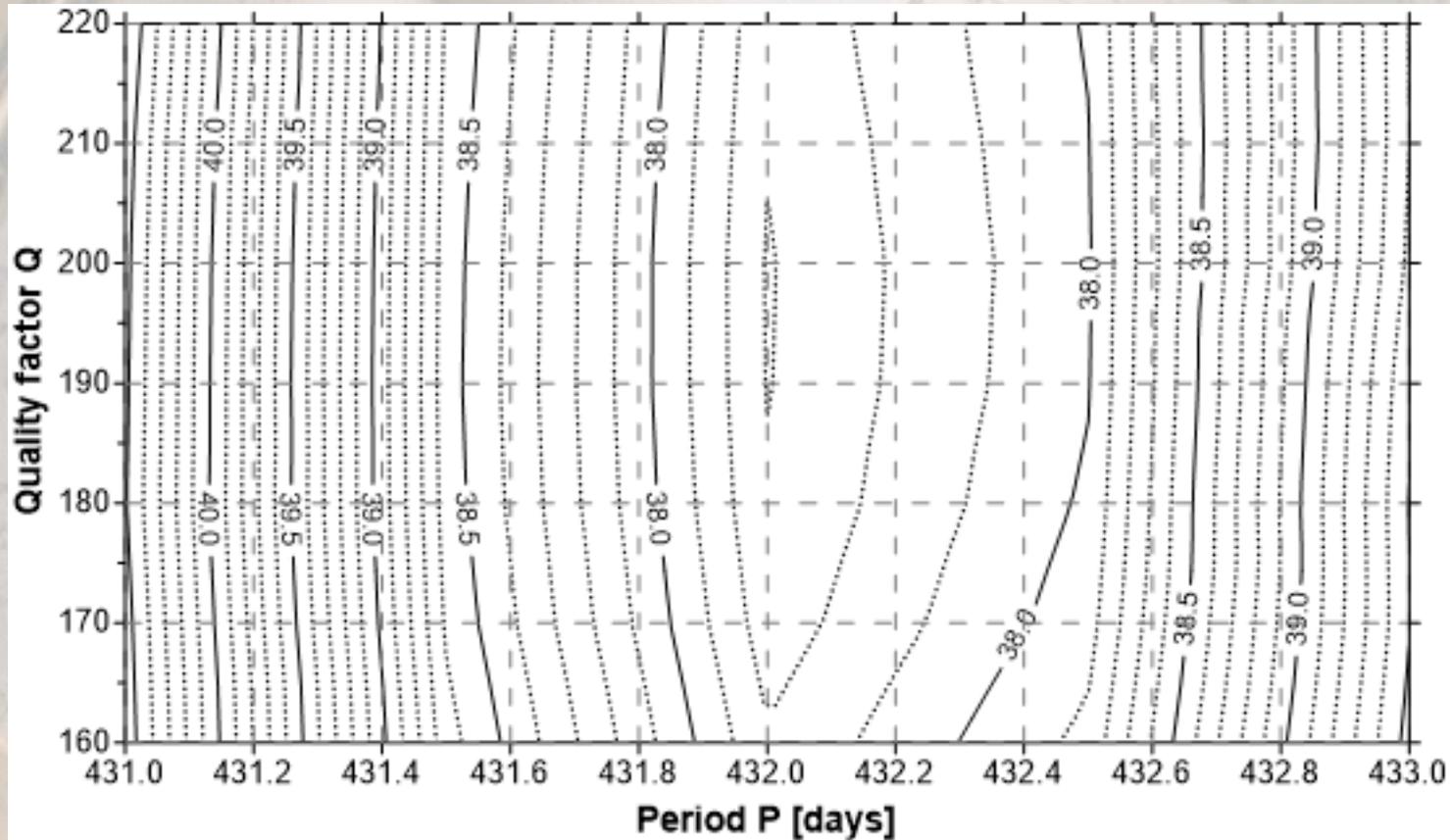
- ◆ We use 4-order Runge-Kutta procedure (in complex form), with 6-hour step:
 - ◆ The initial conditions are chosen to assure the best fit to observations, and also to get rid of 'forbidden' quasi diurnal free motions.
 - ◆ For GMJ (rapid changes of the secular variations of geomagnetic field) we model the excitations as bell-shaped functions centered at GMJ epochs, 200 days wide, complex amplitudes a are estimated to yield the best fit to observations:

$$\chi_{GMJ} = \frac{a}{2} \left[1 + \cos \frac{2\pi(t - t_0)}{200} \right]$$



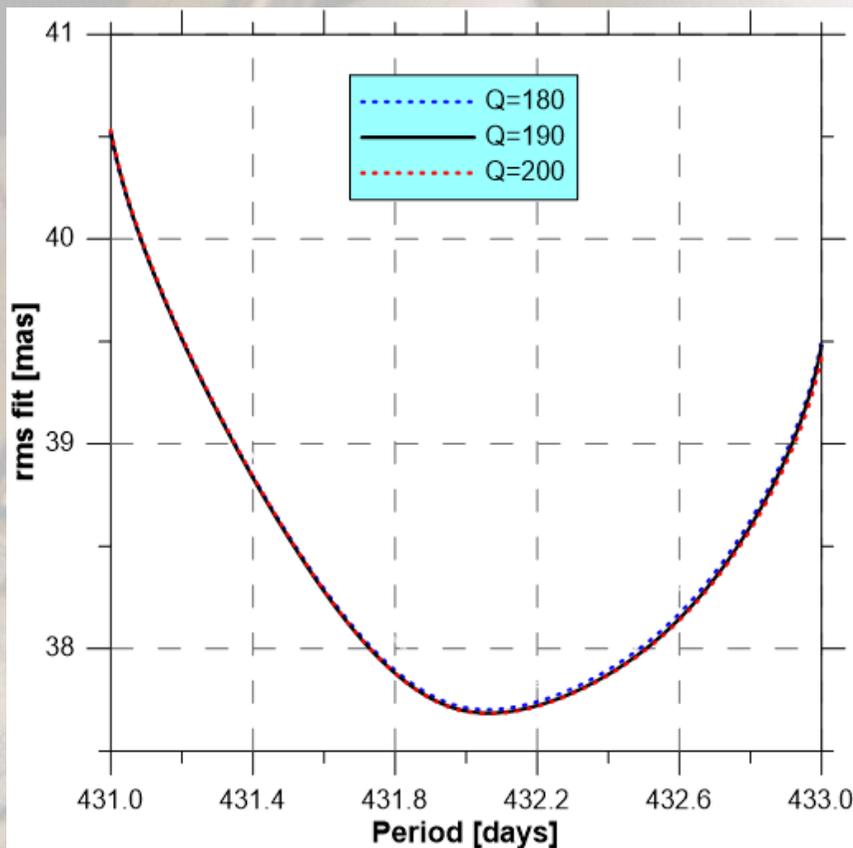
Results for 1974.0-1994.0

A) *only atmosphere + oceans*

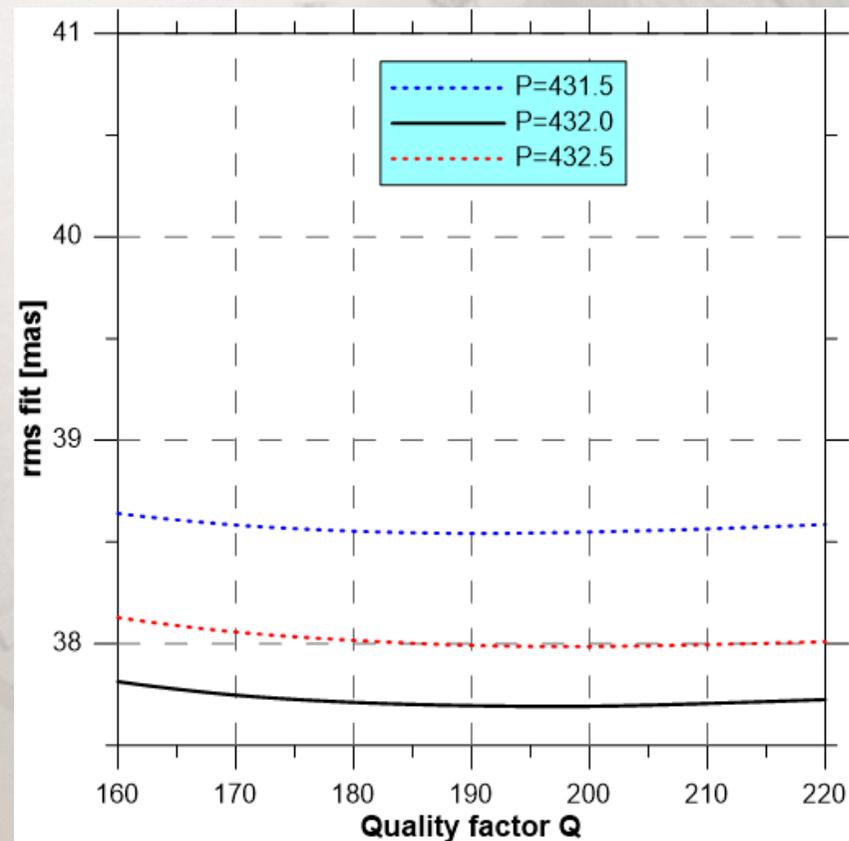


Contour plot of rms fit [mas]

Profiles for 3 different values of P, Q (A+O, 1974.0-1994.0):

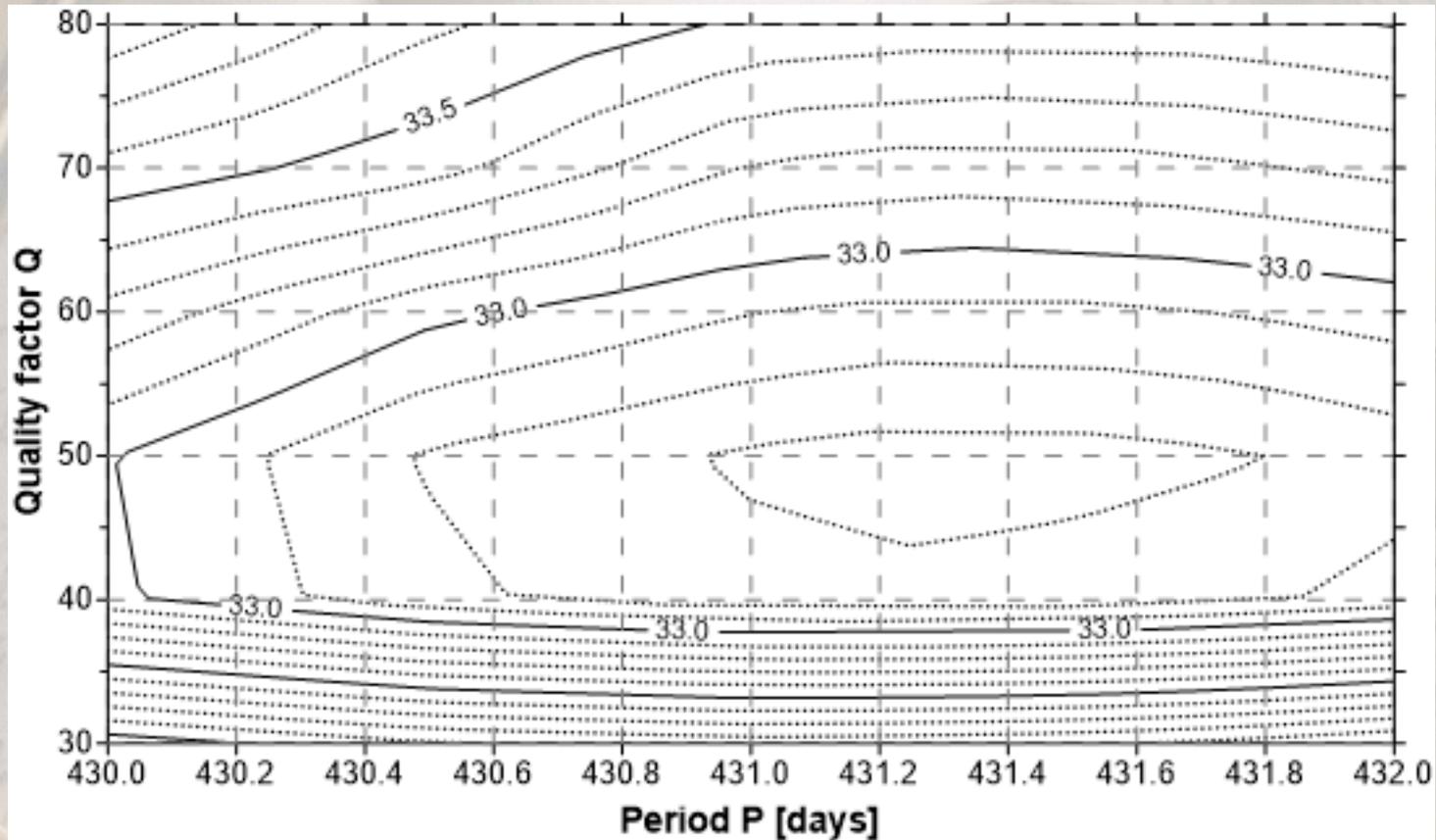


$P=432.13 \pm 0.56$ days



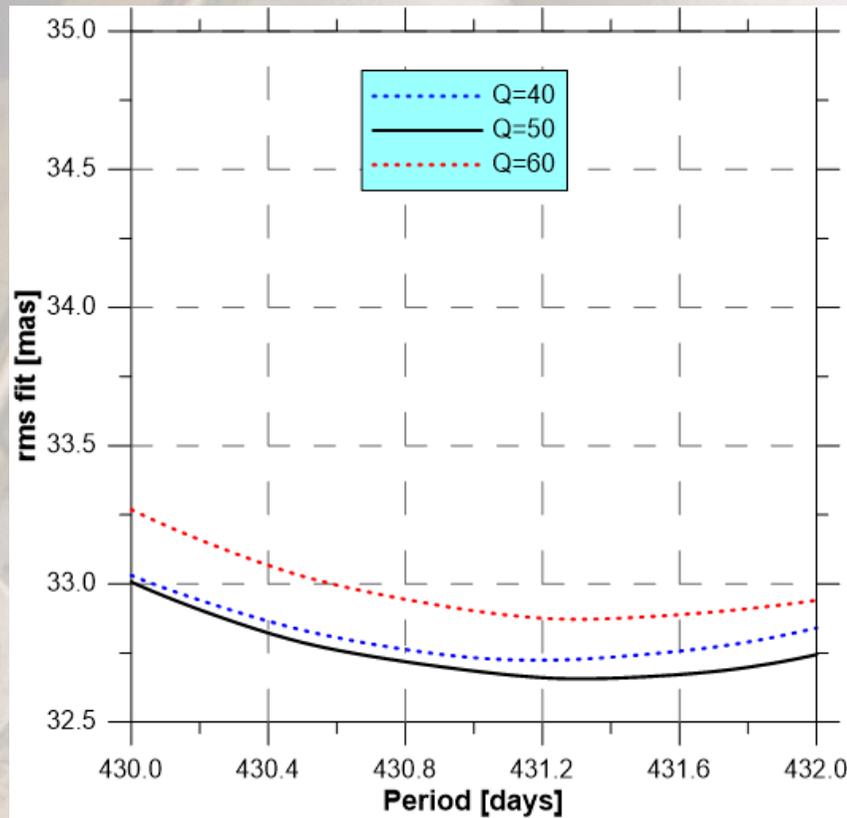
Q=197 (155, 269)

B) atmosphere + oceans + GMJ, 1974.0-1994.0

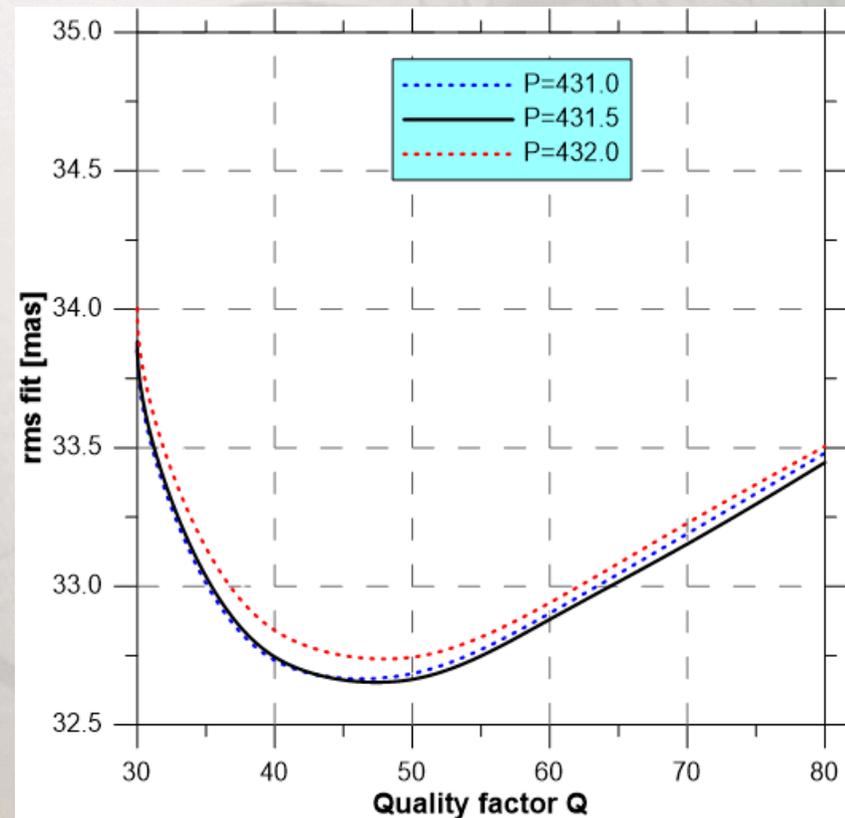


Contour plot of rms fit [mas]

Profiles for 3 different values of P, Q (A+O+G, 1974.0-1994.0):

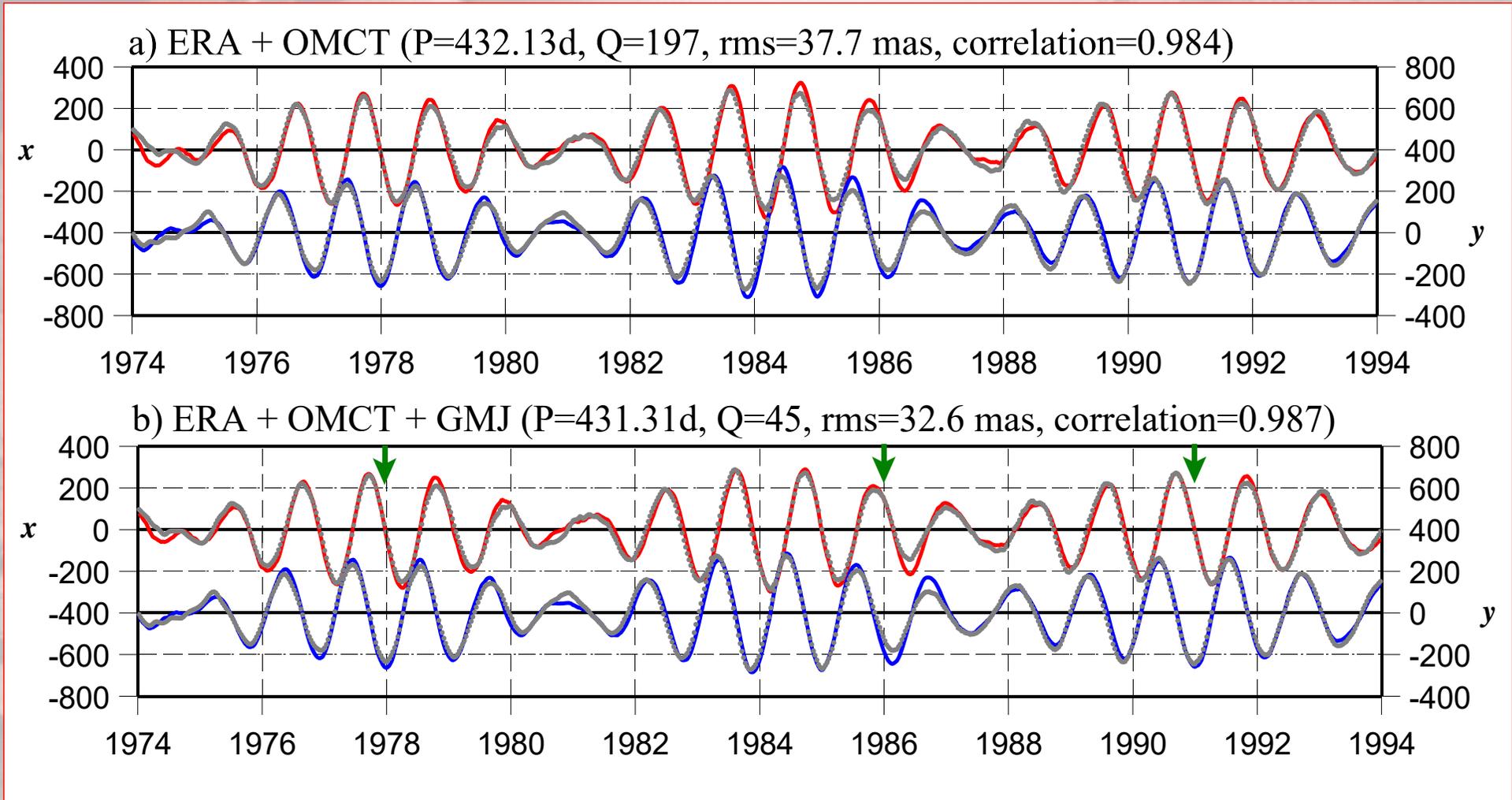


$P=431.31 \pm 0.91$ days



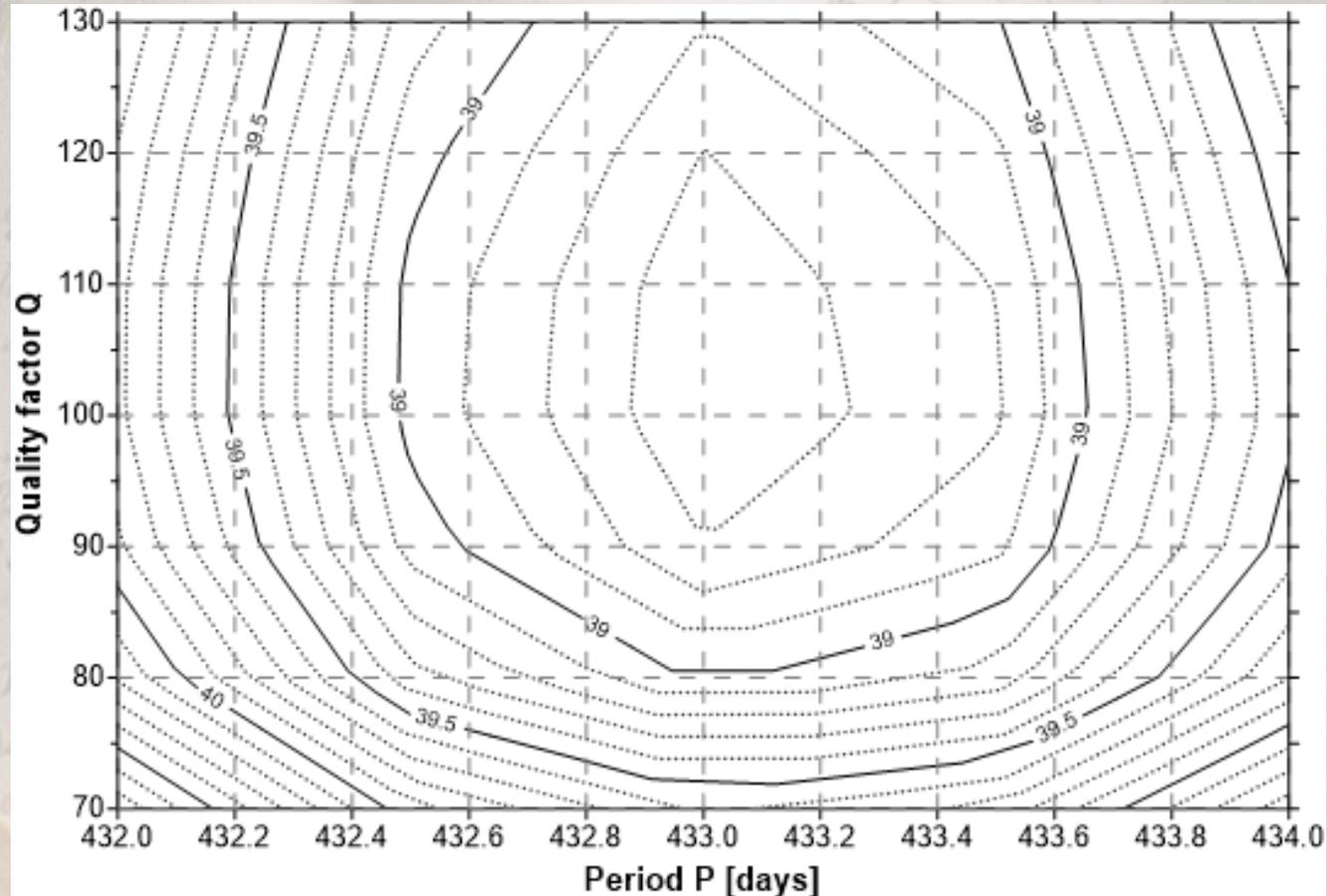
Q=45 (40, 55)

Integrated and observed polar motion, 1974.0-1994.0



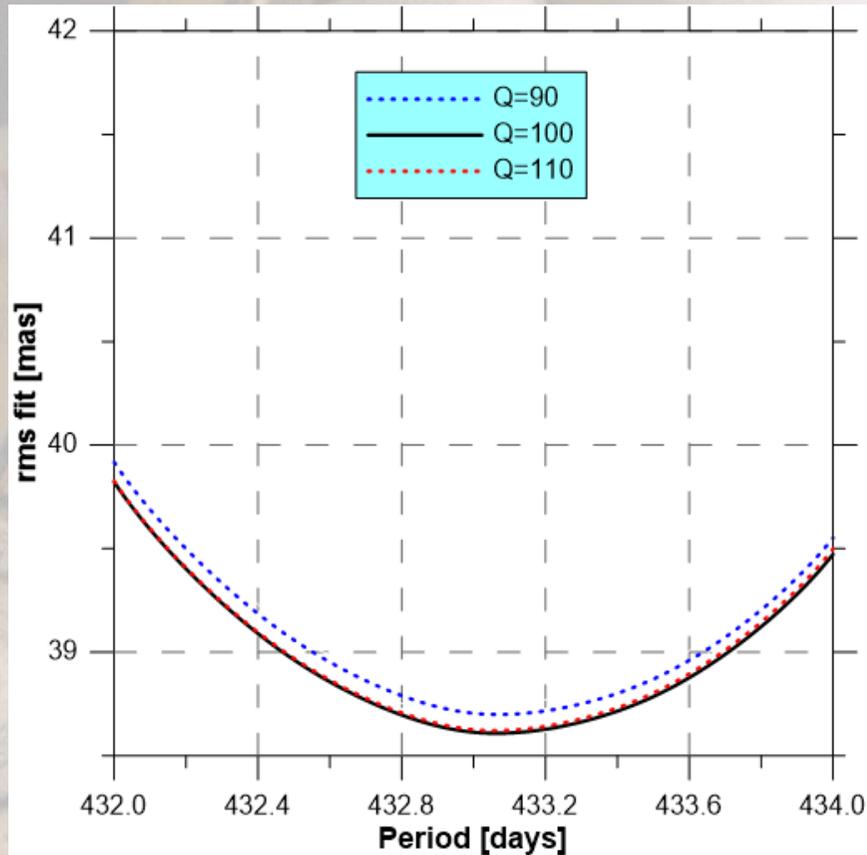
Results for 1994.0-2014.0

A) *only atmosphere + oceans*

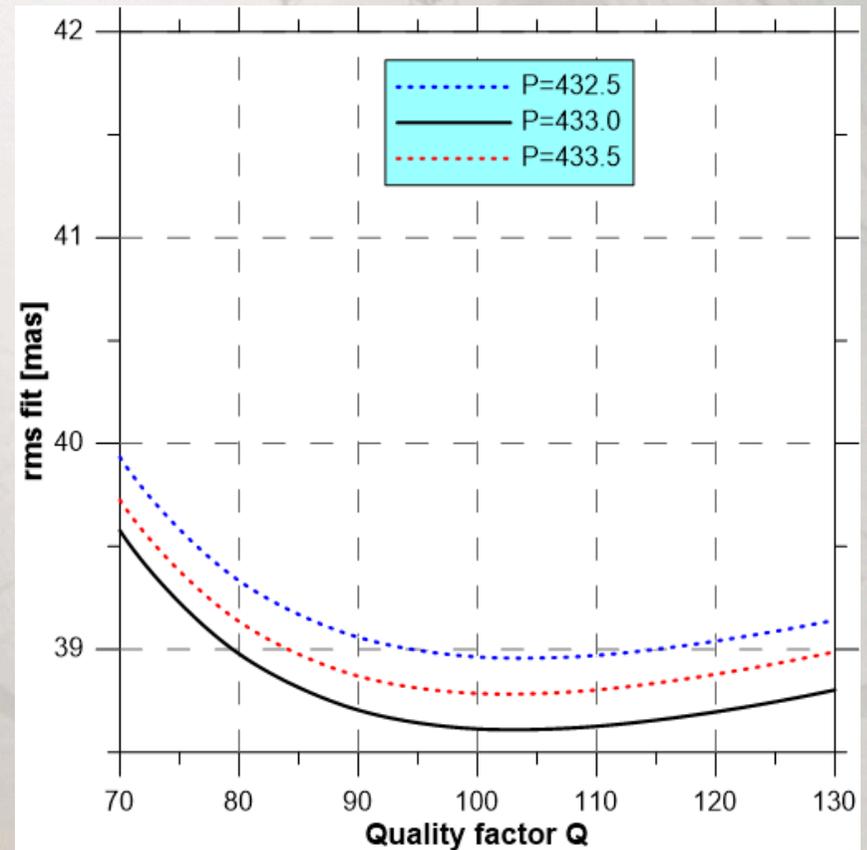


Contour plot of rms fit [mas]

Profiles for 3 different values of P , Q (A+O, 1994.0-2014.0):

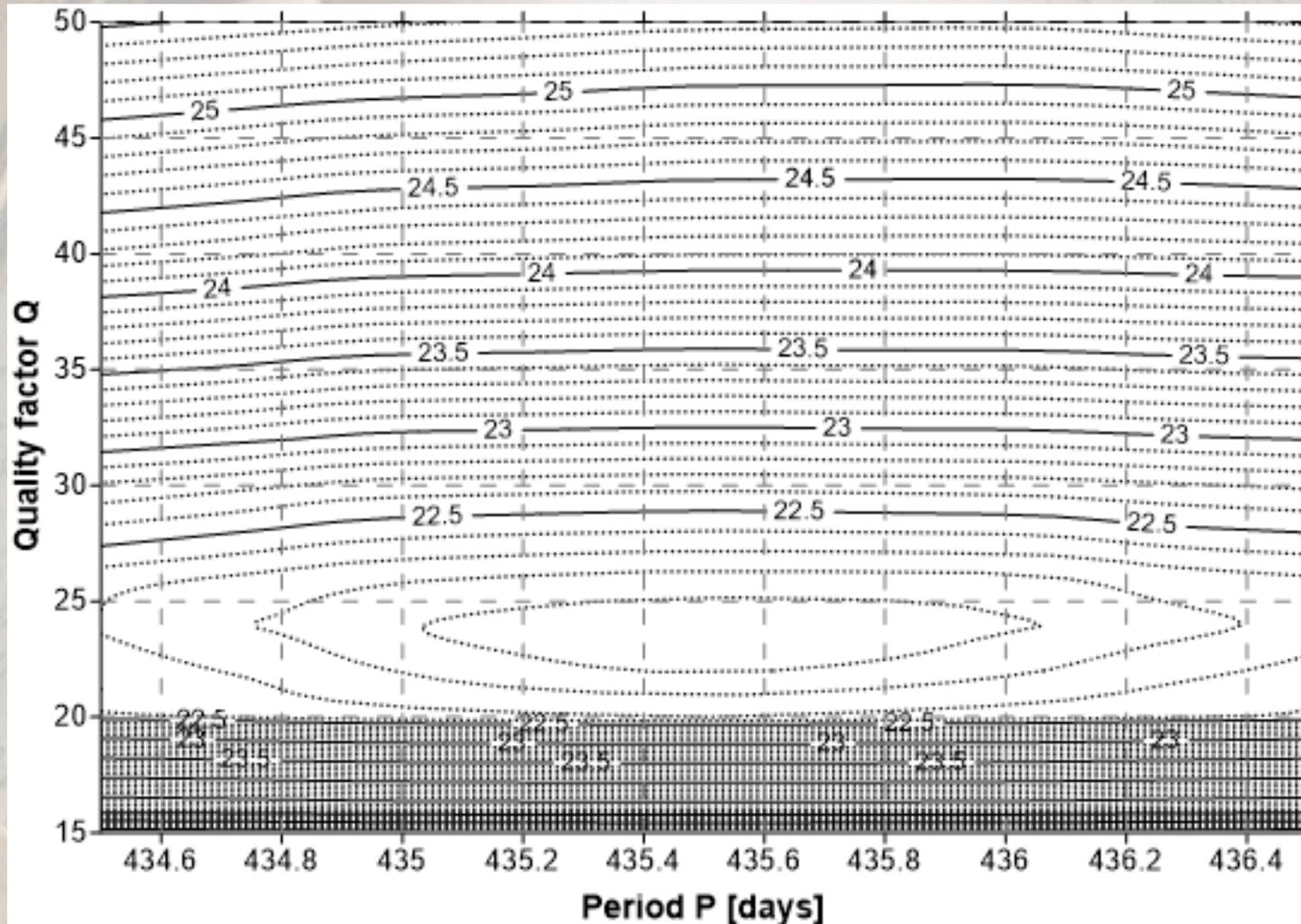


$P=431.09 \pm 0.43$ days



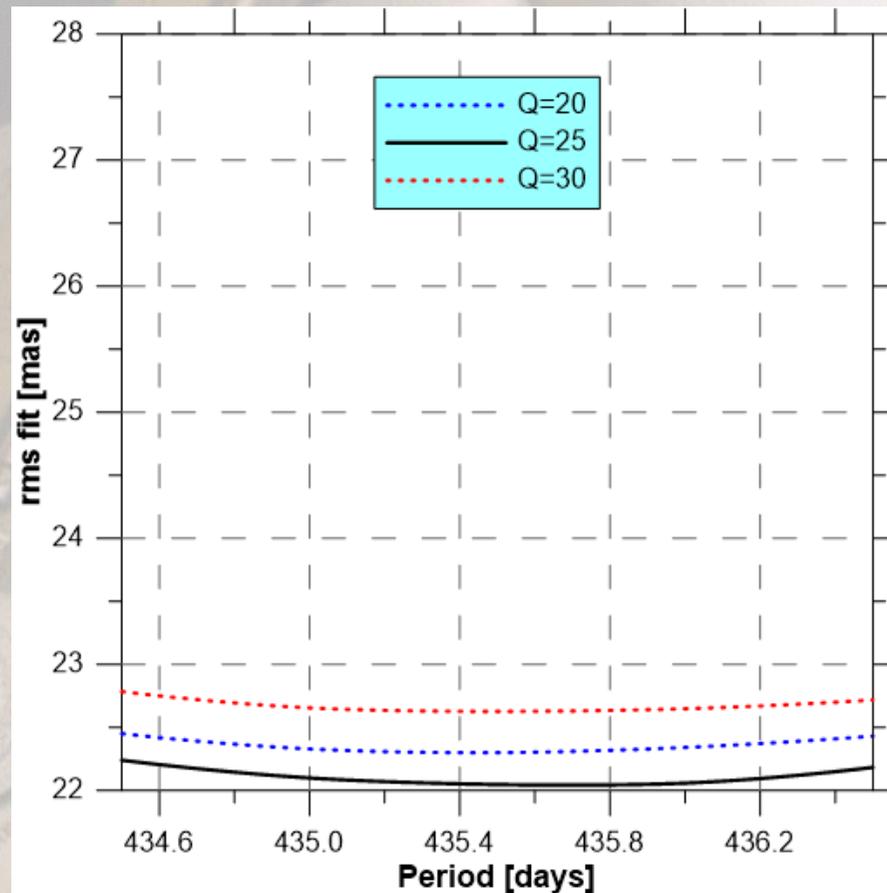
$Q=103$ (85, 130)

B) atmosphere + oceans + GMJ, 1994.0-2014.0

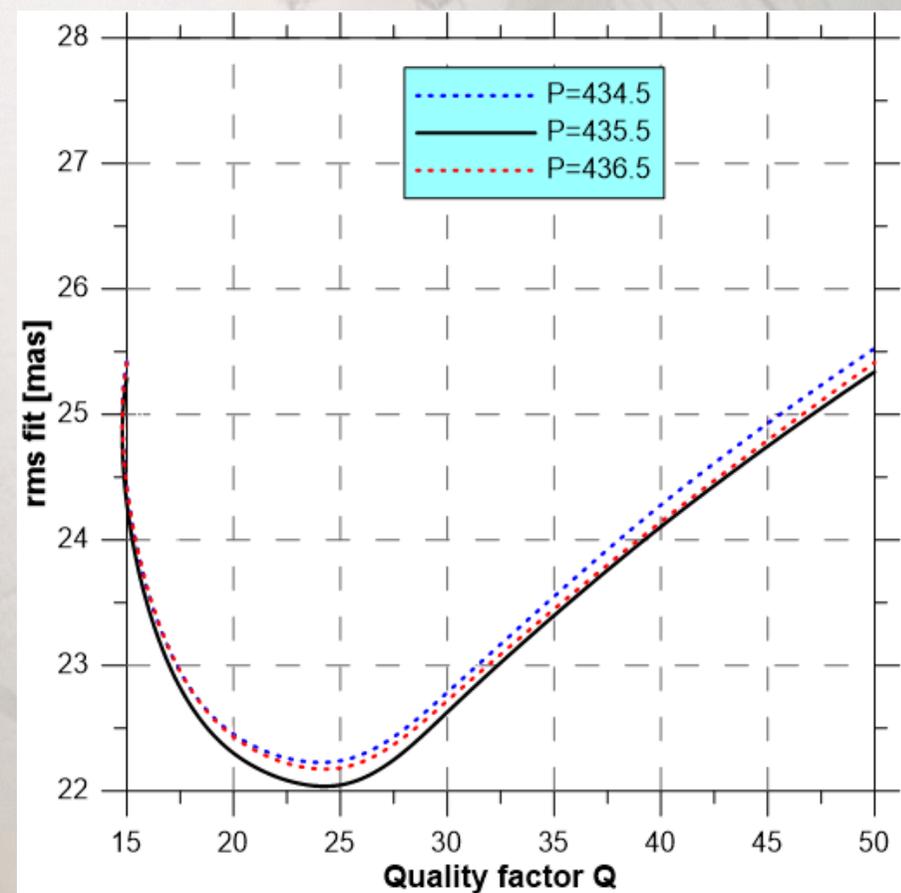


Contour plot of rms fit [mas]

Profiles for 3 different values of P , Q (A+O+G, 1994.0-2014.0):

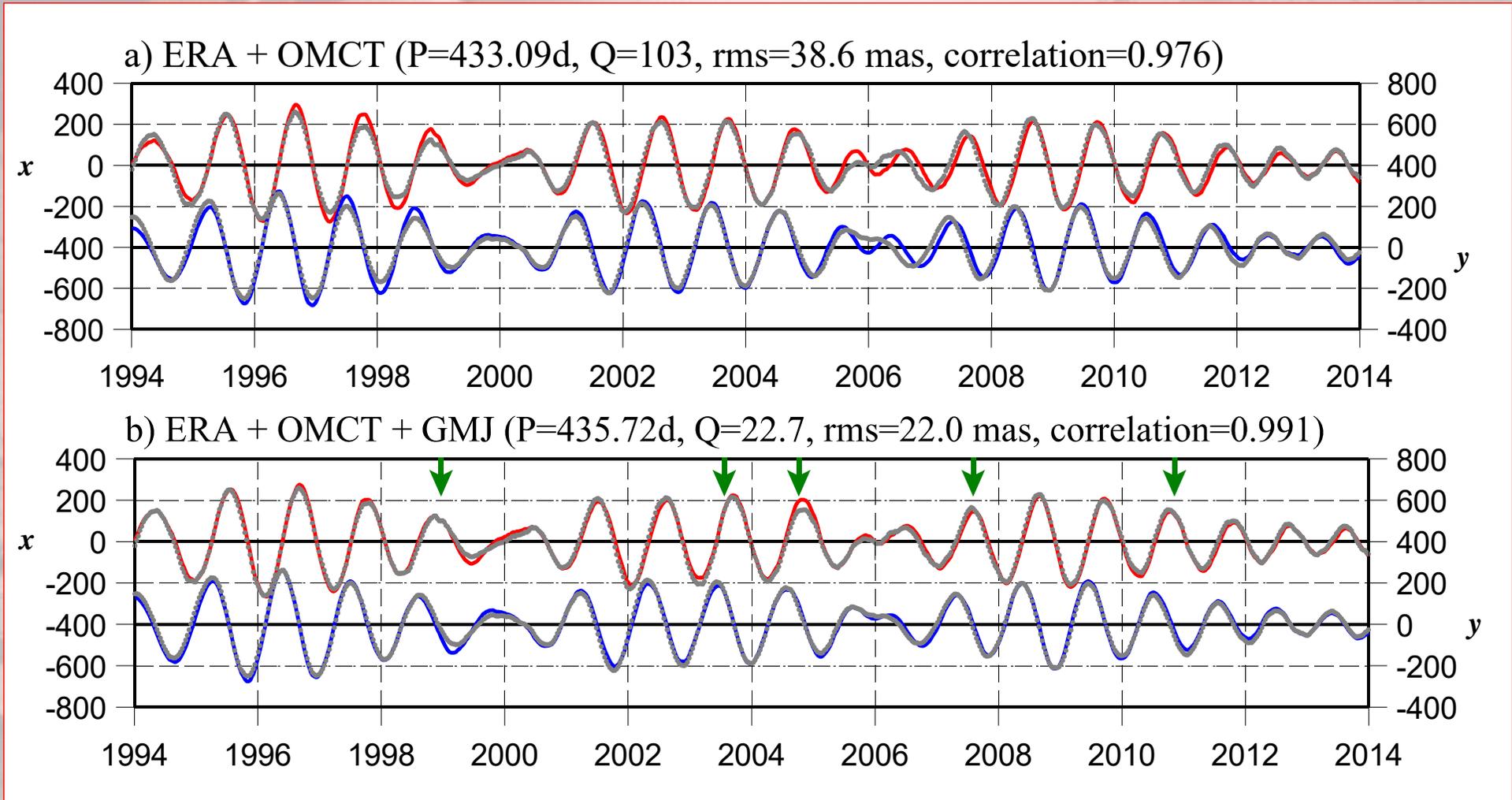


$P=435.72 \pm 0.80$ days



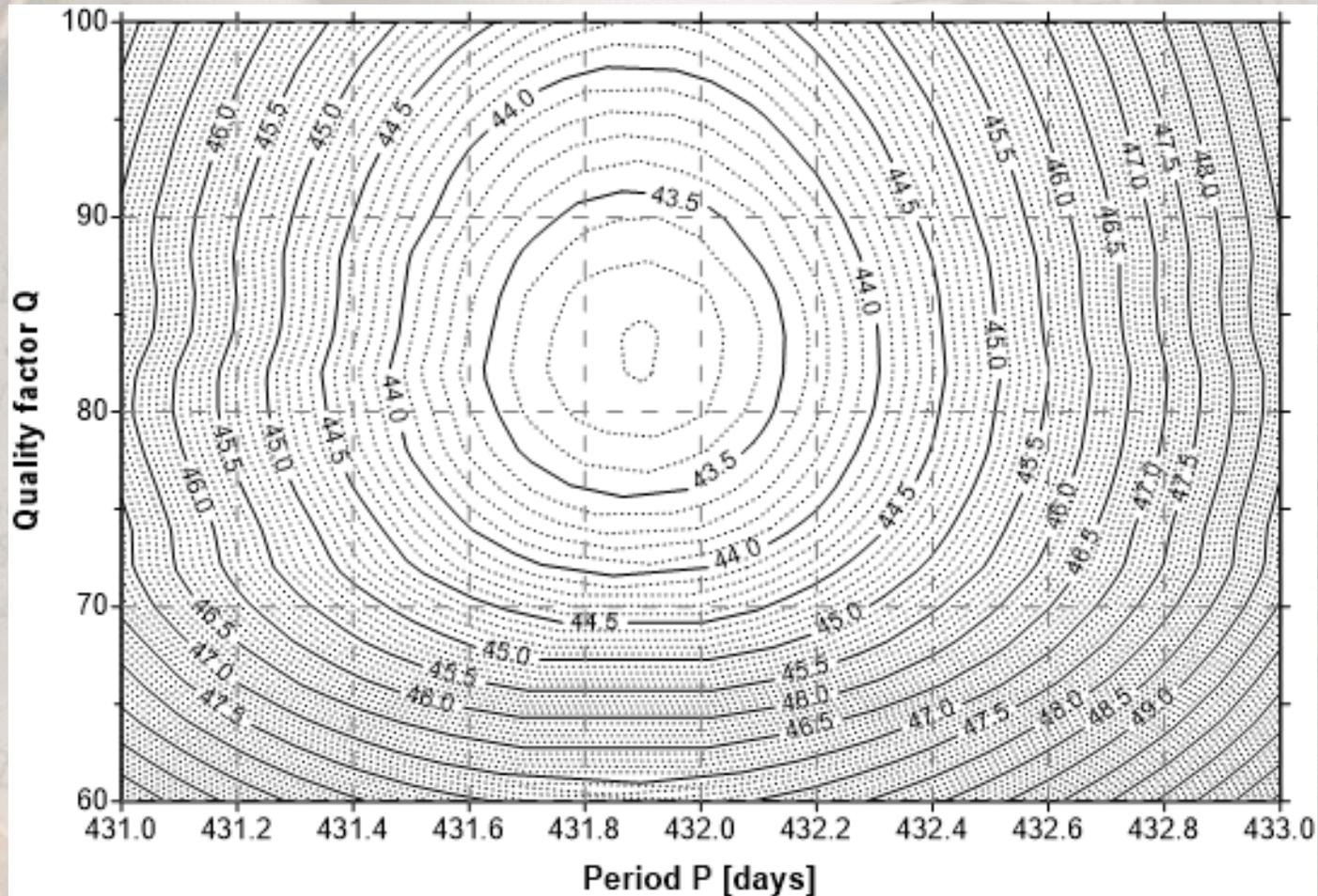
$Q=22.7$ (22.1, 24.6)

Integrated and observed polar motion, 1994.0-2014.0



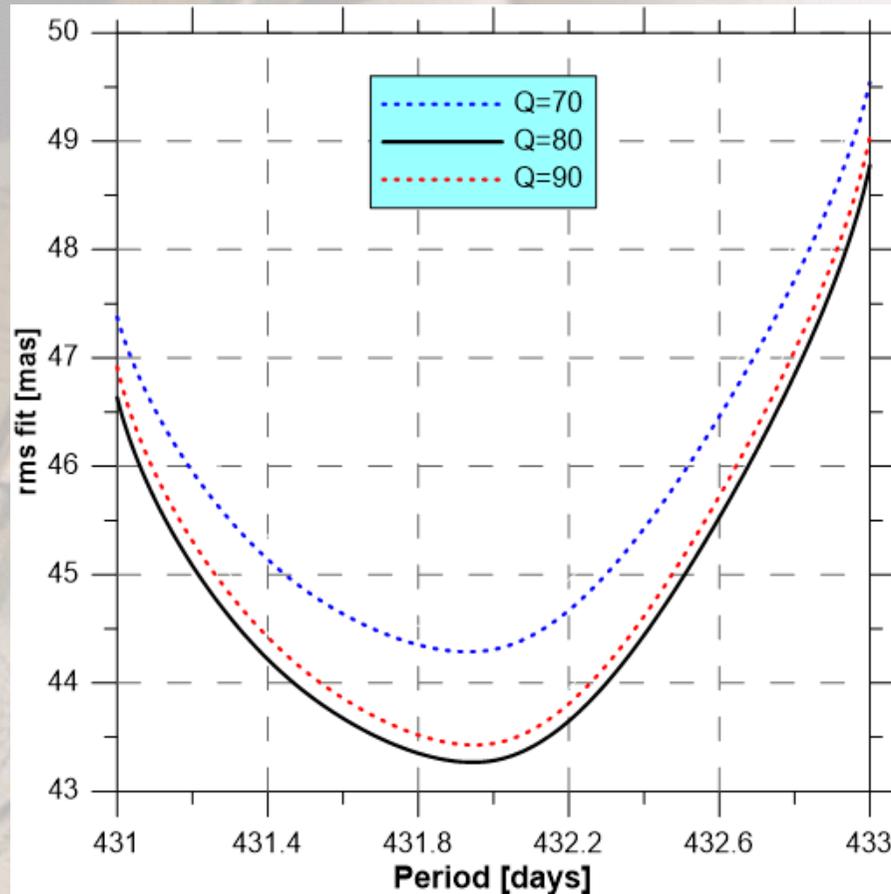
Results for 1974.0-2014.0

A) only atmosphere + oceans

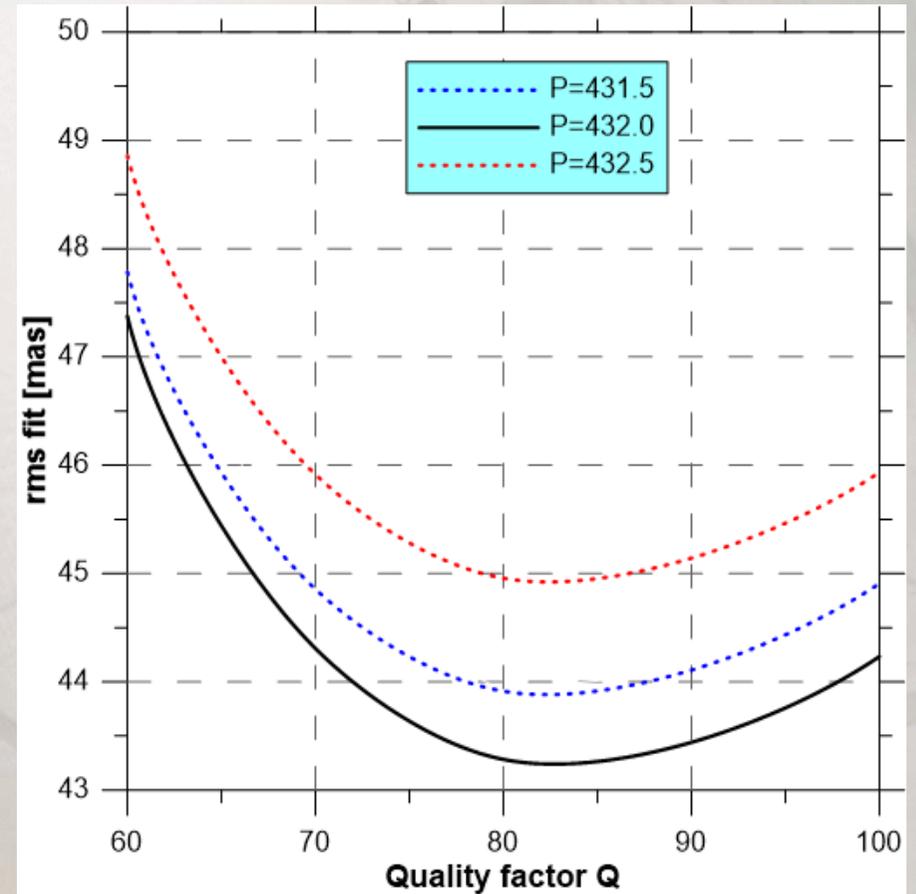


Contour plot of rms fit [mas]

Profiles for 3 different values of P , Q (A+O, 1974.0-2014.0):

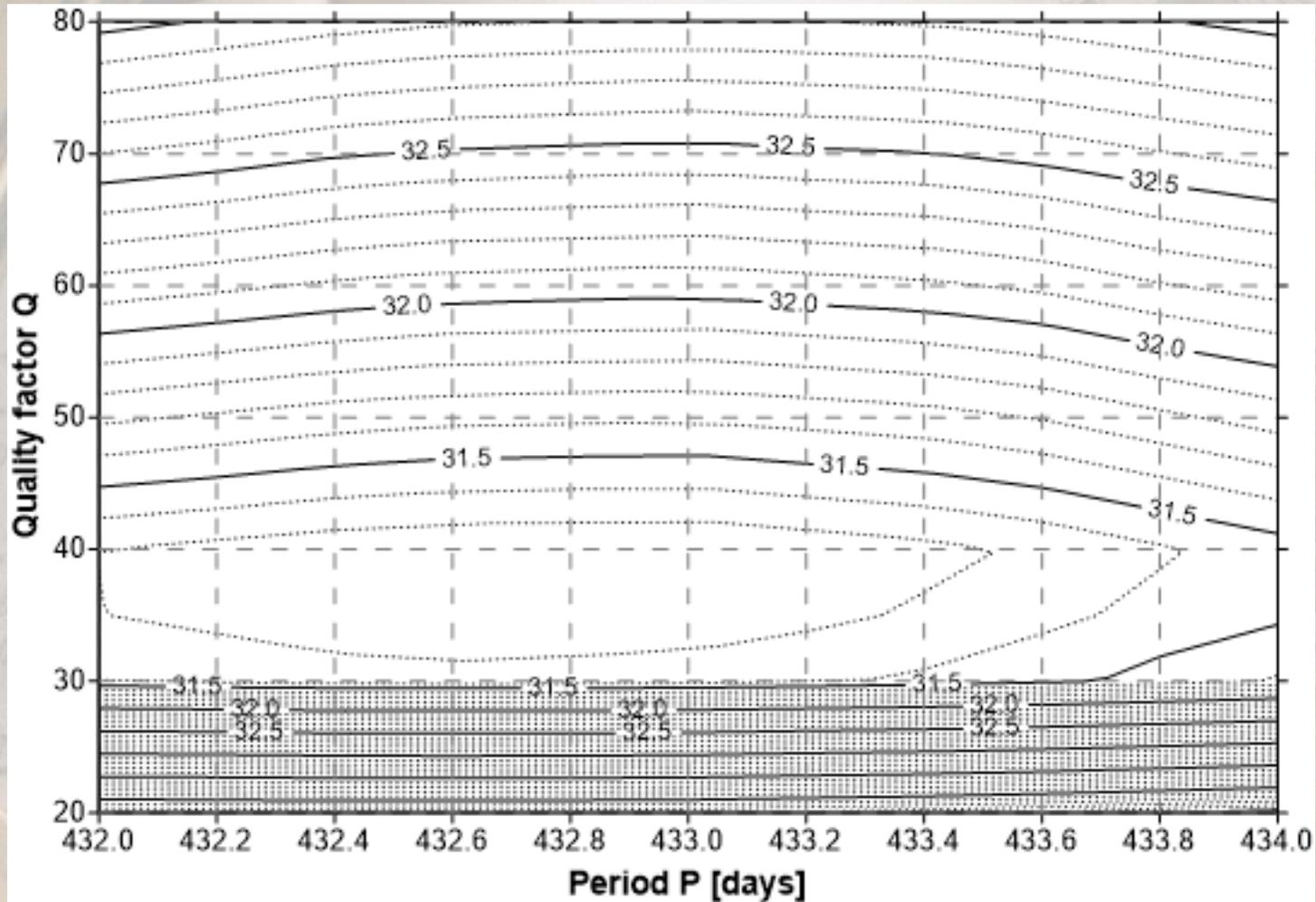


$P=431.88 \pm 0.43$ days



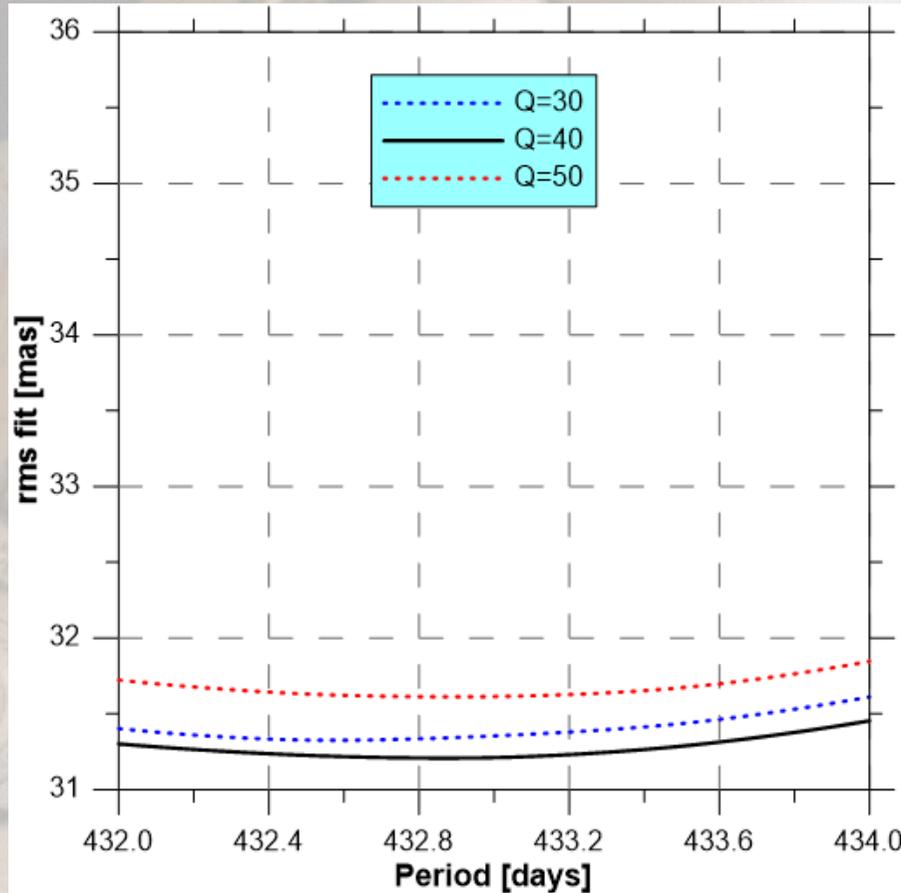
$Q=83$ (76, 90)

B) atmosphere + oceans + GMJ, 1974.0-2014.0

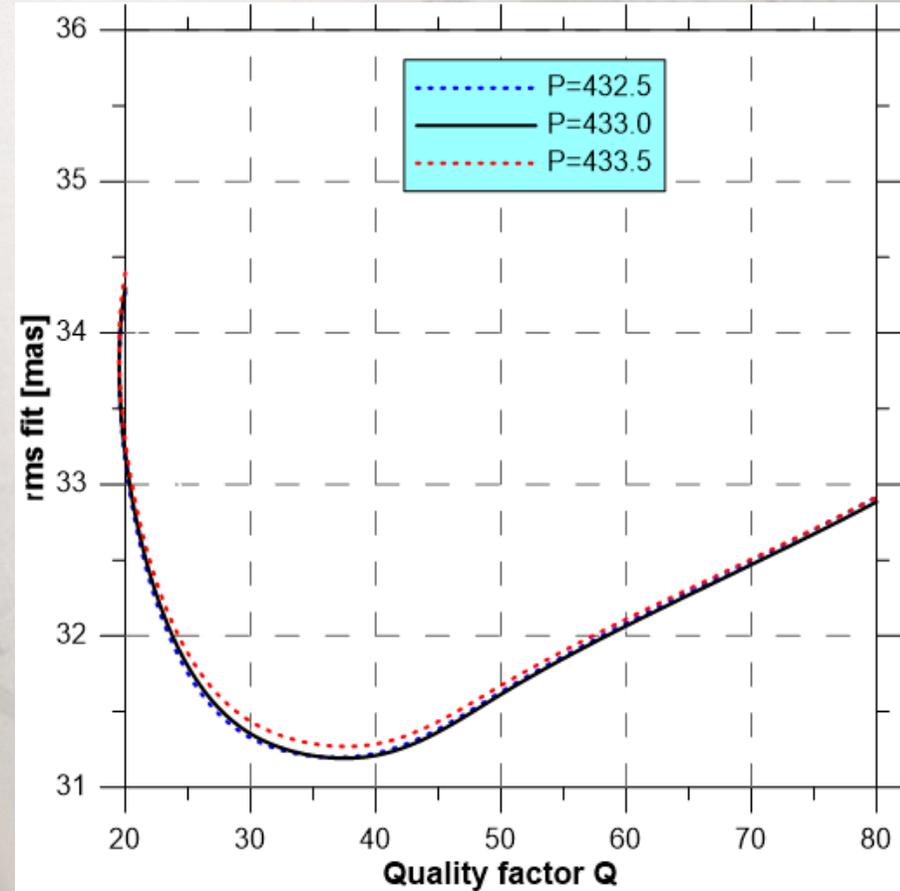


Contour plot of rms fit [mas]

Profiles for 3 different values of P, Q (A+O+G, 1974.0-2014.0):

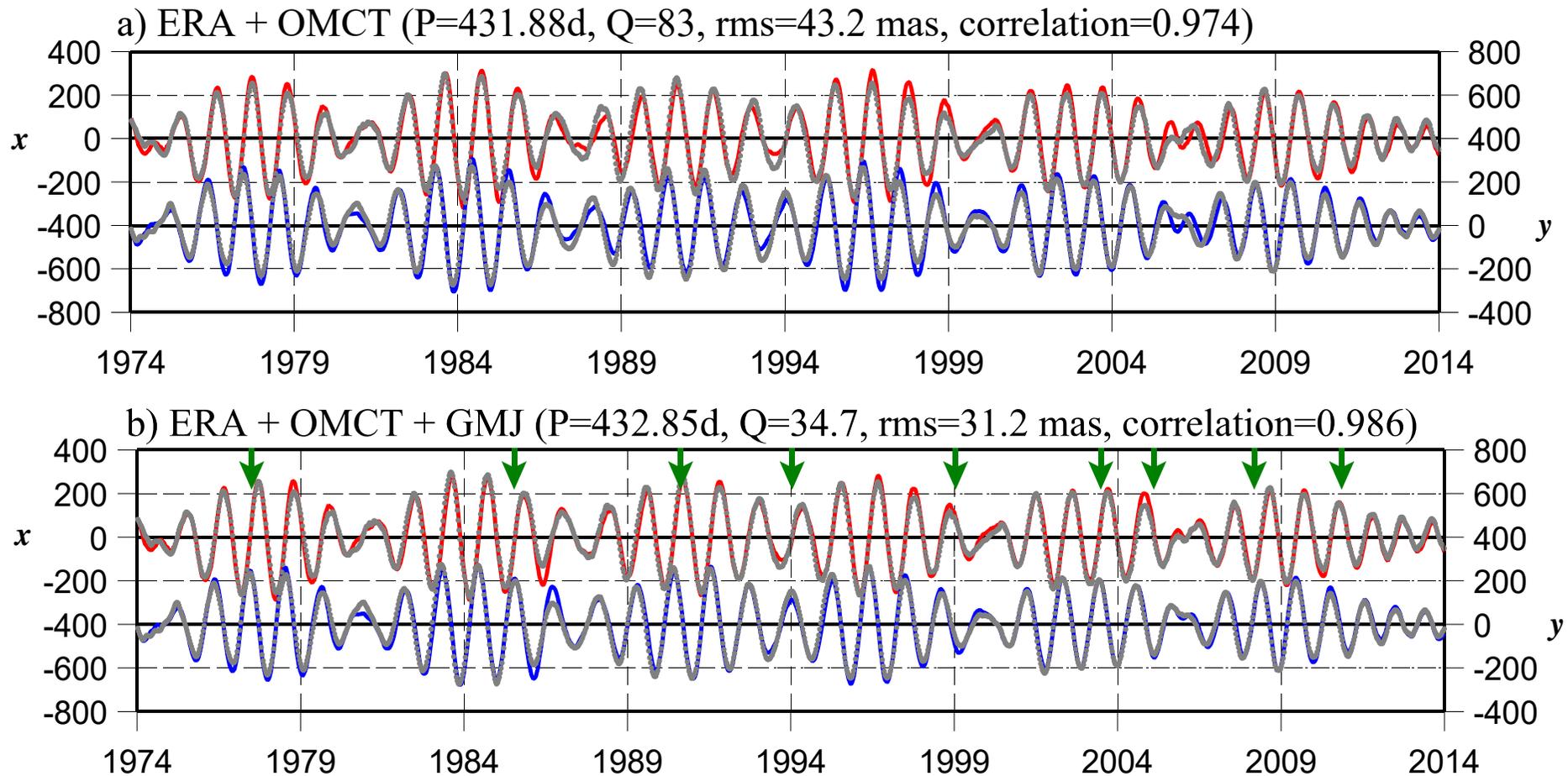


$P=432.85 \pm 0.99$ days



$Q=34.7$ (31.2, 39.5)

Integrated and observed polar motion, 1974.0-2014.0



Summary of the results:

Results of Chandler wobble period P (in days) and quality factor Q , obtained with only atmospheric and oceanic excitations (A+O), and with GMJ added (A+O+G). Root-mean-square fit rms between integrated and observed values (in mas) are also shown.

interval	A+O			A+O+G		
	P	Q	rms	P	Q	rms
1974.0-1994.0	432.13±0.56	197 (155, 269)	37.7	431.31±0.91	45 (40, 55)	32.6
1994.0-2014.0	431.09±0.43	103 (85, 130)	38.6	435.72±0.80	22.7 (22.1, 24.6)	22.7
1974.0-2014.0	431.88±0.43	83 (76, 90)	43.2	432.85±0.99	34.7 (31.2, 39.5)	31.2

Preferred values

Conclusions:

- ◆ Geophysical excitations yield significant contribution to polar motion;
- ◆ Additional excitation by GMJ substantially improves the agreement with observations in all intervals studied;
 - ◆ determination of Q -factor is improved, and yields lower values (stronger damping):
 - ◆ dampings between GMJ events are stronger than average value over the whole interval,
 - ◆ determination of the period P is less accurate, but consistent with its values without GMJ:
 - ◆ it is based on short time intervals between individual GMJ events.
- ◆ Our preferred values are $P=431.88\pm 0.43$, $Q=34.7$ (31.2,39.5)

THANK YOU FOR YOUR ATTENTION!

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