

# The Fe $K\alpha$ line and supermassive black holes

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and

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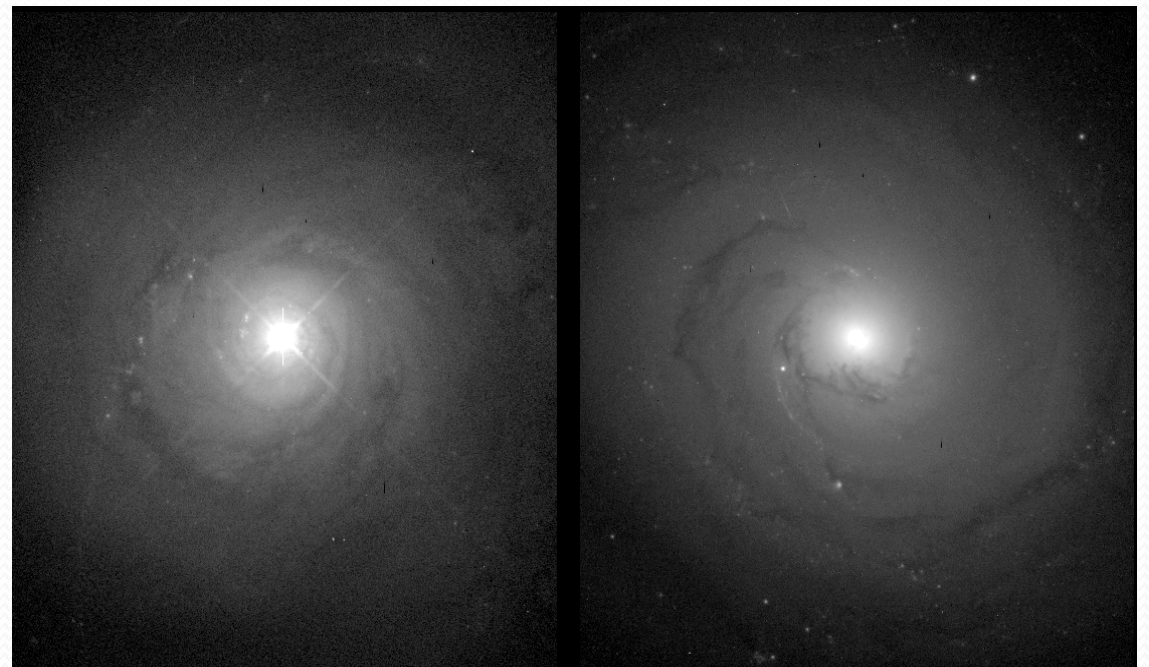
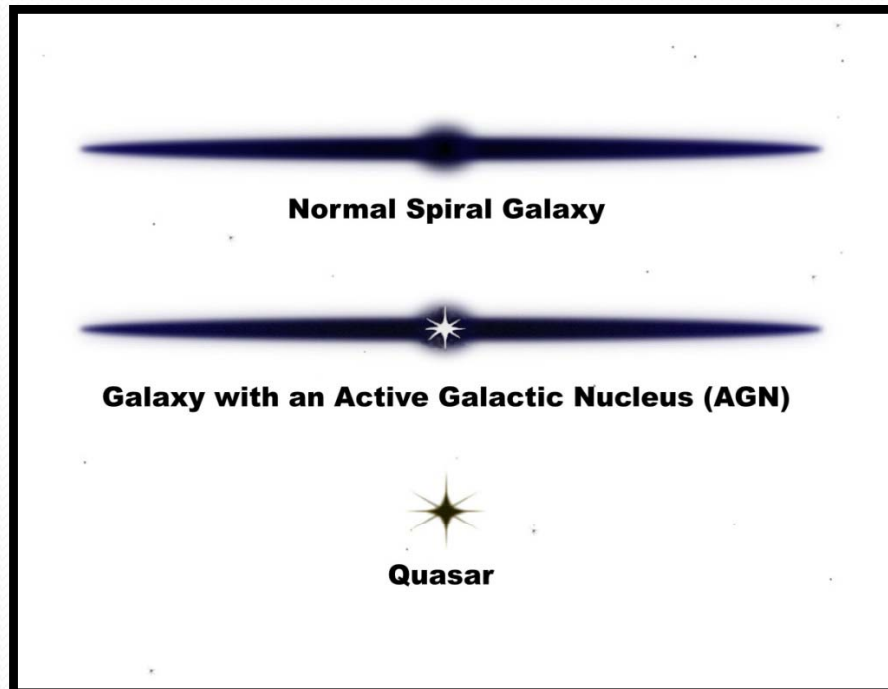
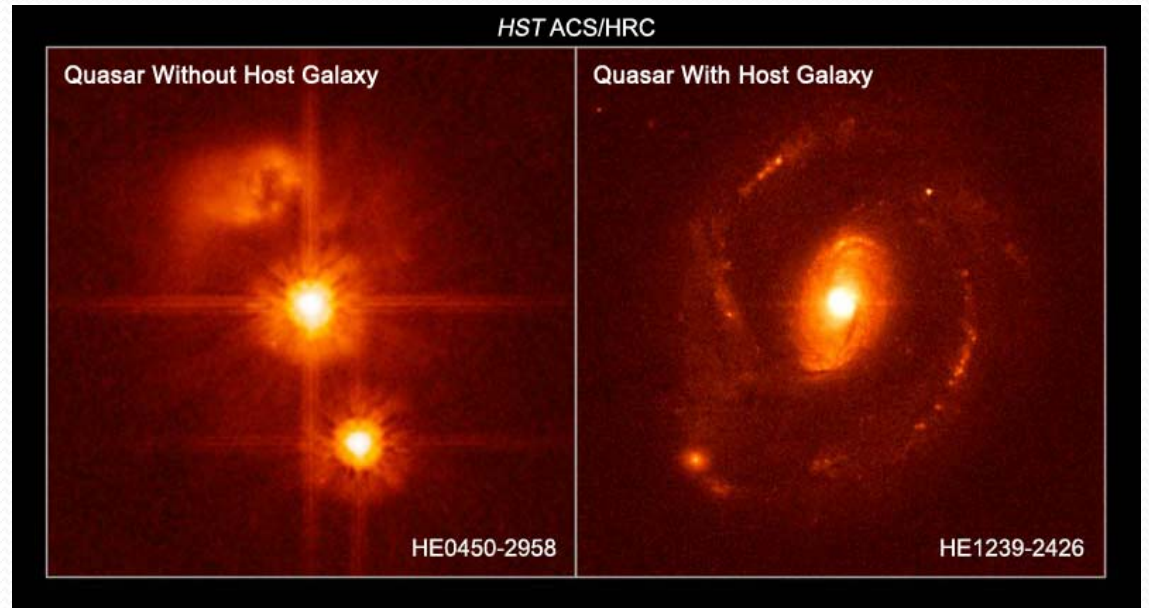
Astronomical Observatory,  
11060 Belgrade, Serbia

# Outline

- Active Galactic Nuclei (AGN)
- Supermassive Black Holes (SMBH)
- Fe  $K\alpha$  spectral line
- Our investigations and results
- Conclusions
- References

# Active Galaxies and Quasars

- Small highly variable and very bright core embedded in an otherwise typical galaxy



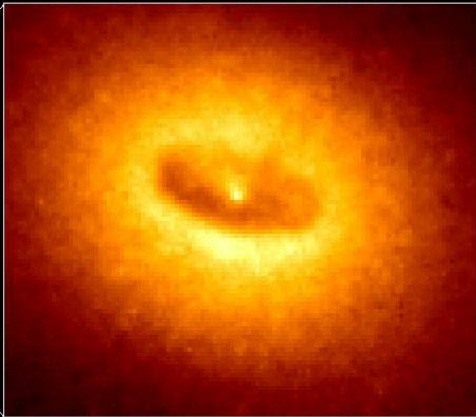
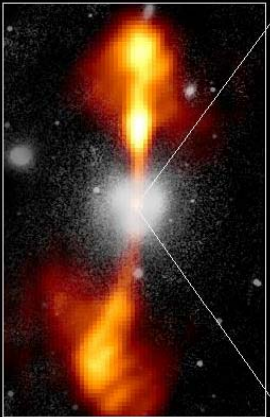
Left: NGC 5548 (Seyfert galaxy)  
Right: NGC 3277 (regular galaxy)

# Core of Galaxy NGC 4261

Hubble Space Telescope  
Wide Field / Planetary Camera

Ground-Based Optical/Radio Image

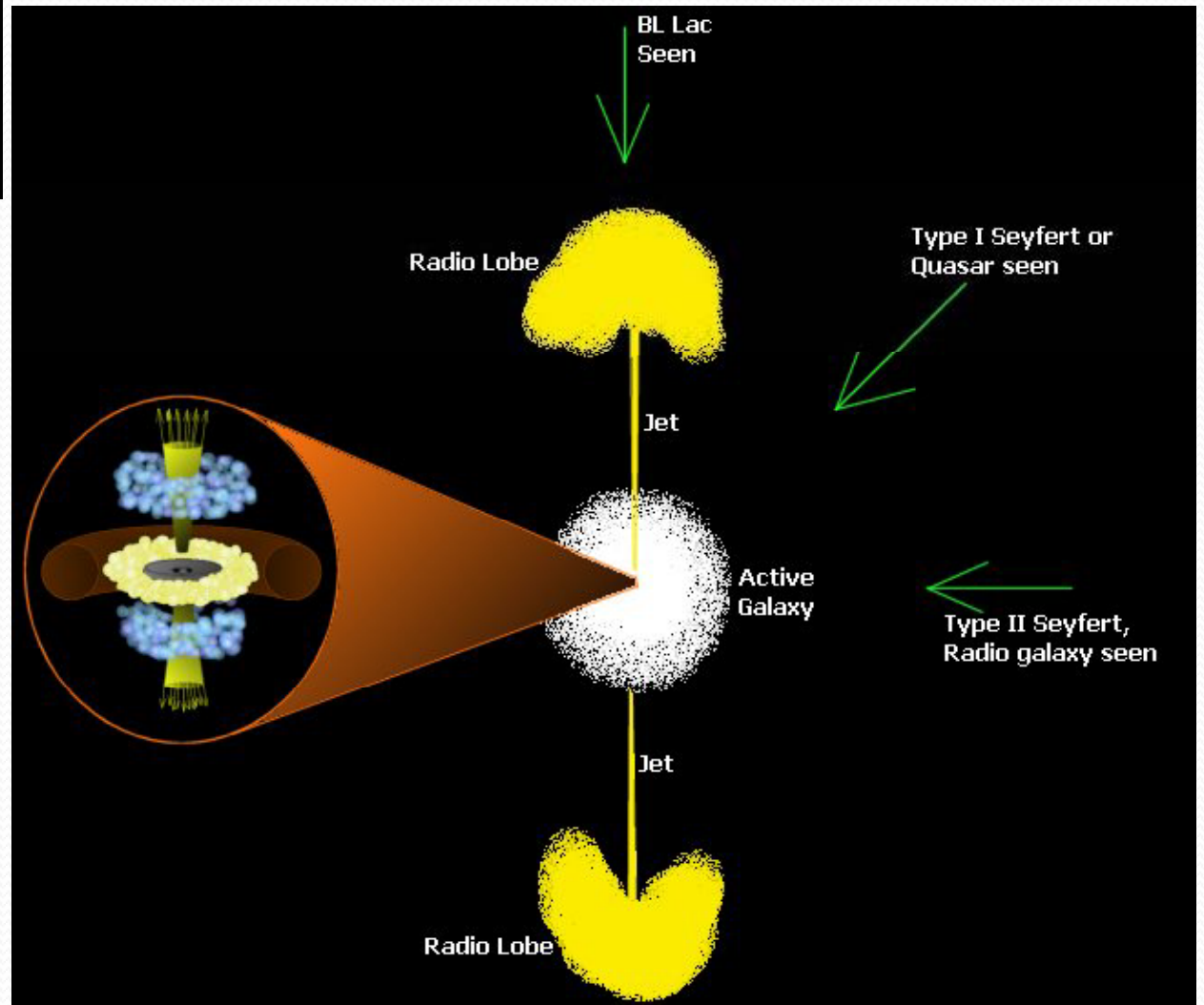
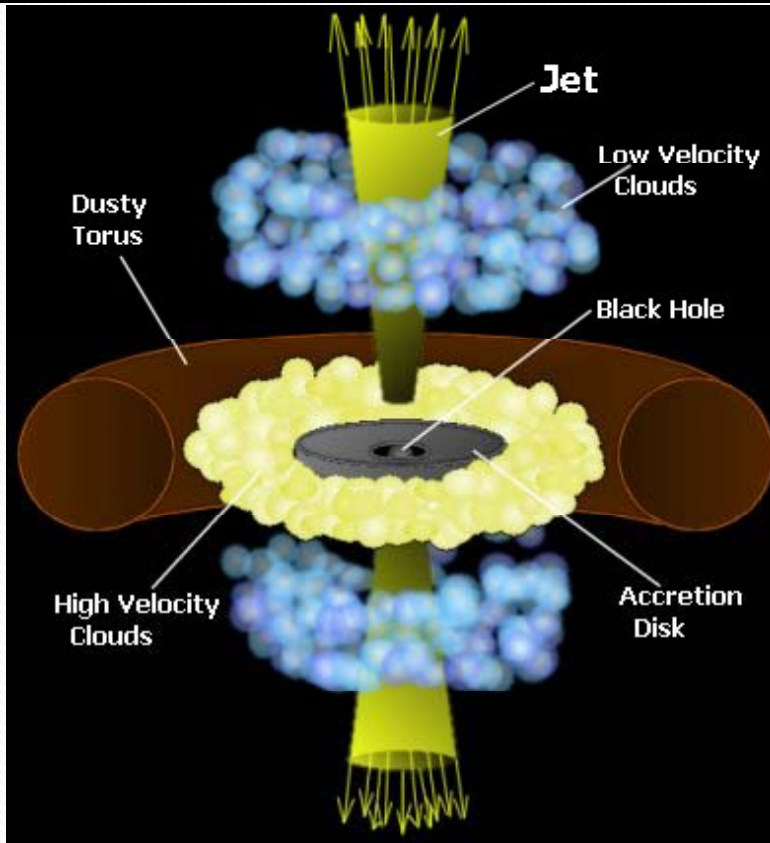
HST Image of a Gas and Dust Disk



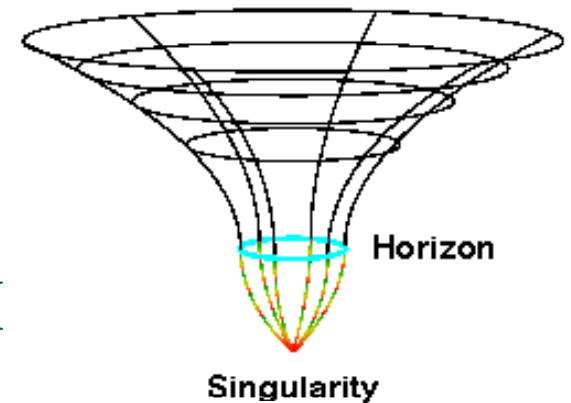
380 Arc Seconds  
88,000 LIGHTYEARS

17 Arc Seconds  
400 LIGHTYEARS

# Unified model of AGN



# Space-time geometry in Vicinity of Supermassive BH



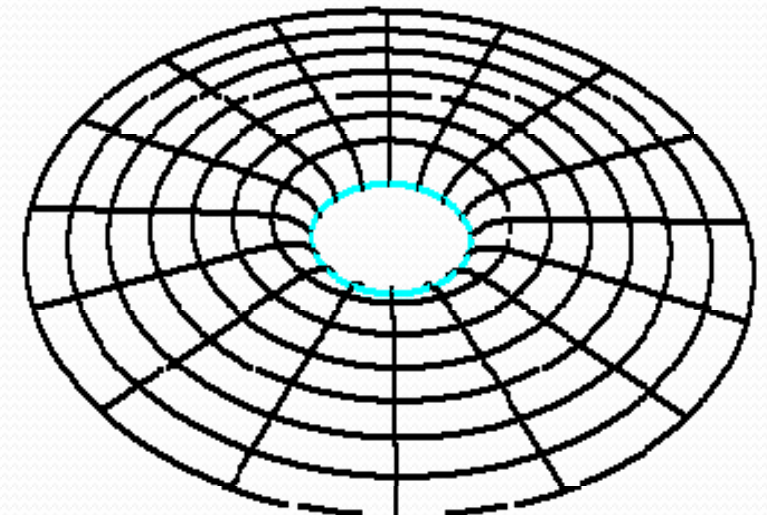
## 1. Schwarzschild metric – nonrotating BH

$$ds^2 = \left( \frac{1}{1 - \frac{R_S}{r}} \right) dr^2 - \left( 1 - \frac{R_S}{r} \right) c^2 dt^2 + r^2 (d\theta^2 + \sin^2 \theta d\phi^2)$$

- Schwarzschild radius:  $R_S = \frac{2GM}{c^2}$
- gravitational radius:  $R_g = \frac{R_S}{2} = \frac{GM}{c^2}$

$G$  – Newton's gravitational constant

$c$  – speed of light,  $M$  – mass of BH



## 2. Kerr metric – rotating BH

- in units where  $G = c = 1$  :

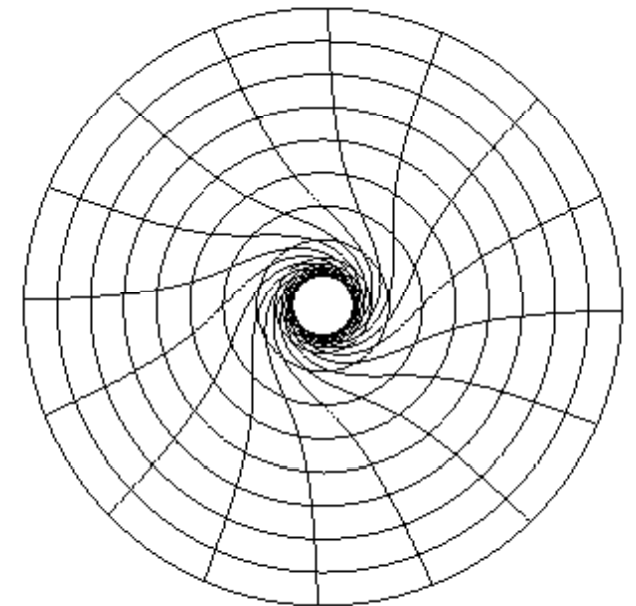
$$ds^2 = - \left( 1 - \frac{2Mr}{\Sigma} \right) dt^2 - \frac{4Mar}{\Sigma} \sin^2 \theta dt d\phi + \frac{A}{\Sigma} \sin^2 \theta d\phi^2 + \frac{\Sigma}{\Delta} dr^2 + \Sigma d\theta^2,$$

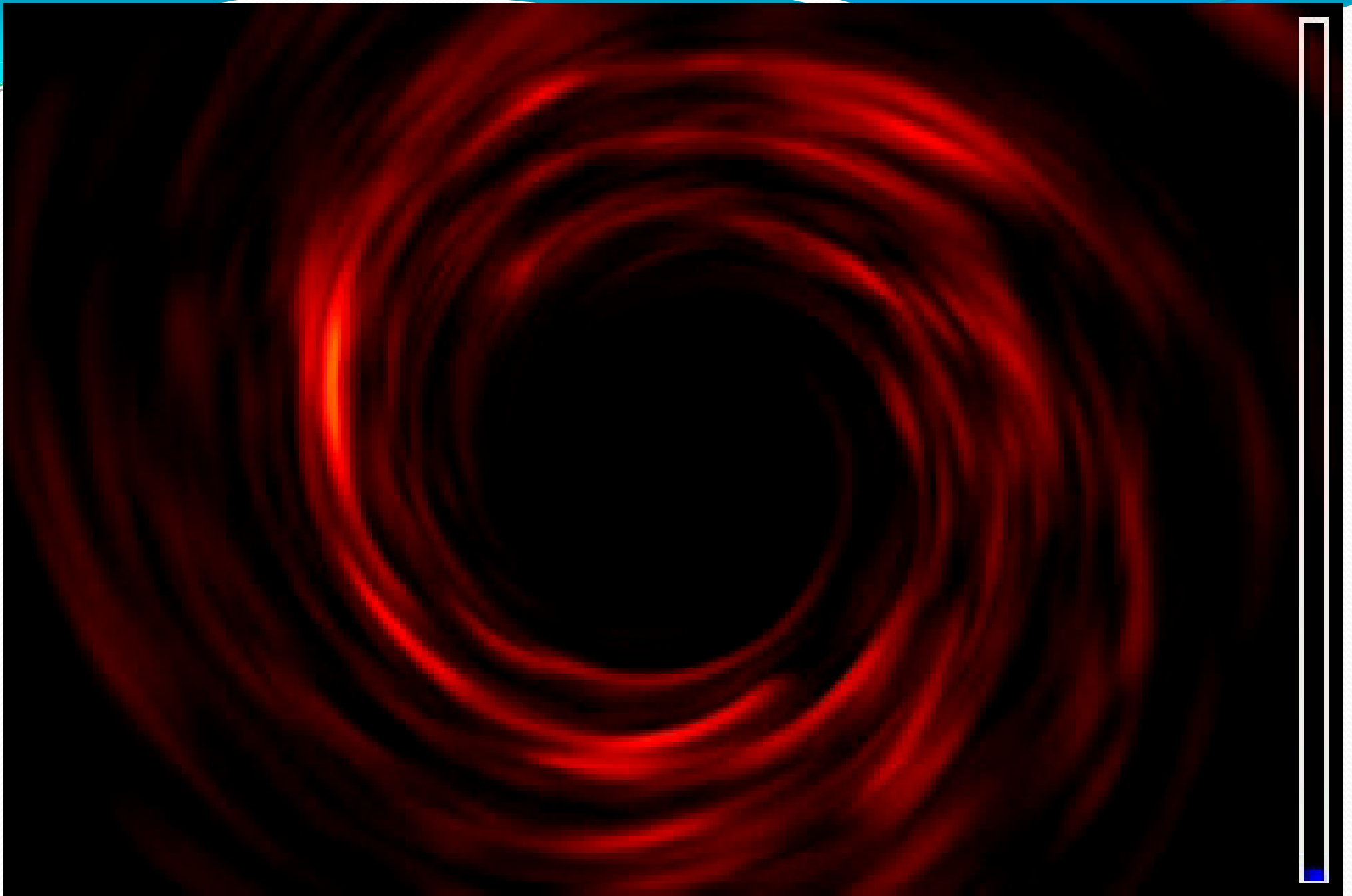
$$\Sigma = r^2 + a^2 \cos^2 \theta, \quad \Delta = r^2 + a^2 - 2Mr, \quad A = (r^2 + a^2)^2 - a^2 \Delta \sin^2 \theta$$

- horizon of BH:  $\Delta = 0 \Rightarrow r_h = M + \sqrt{M^2 - a^2}$
- radius of marginally stable orbit:

$$r^2 - 6Mr \mp 8a\sqrt{Mr} - 3a^2 = 0 \Rightarrow$$

$$\Rightarrow R_{ms} = \begin{cases} 6M, & a = 0 \\ M, & a = M \end{cases}$$

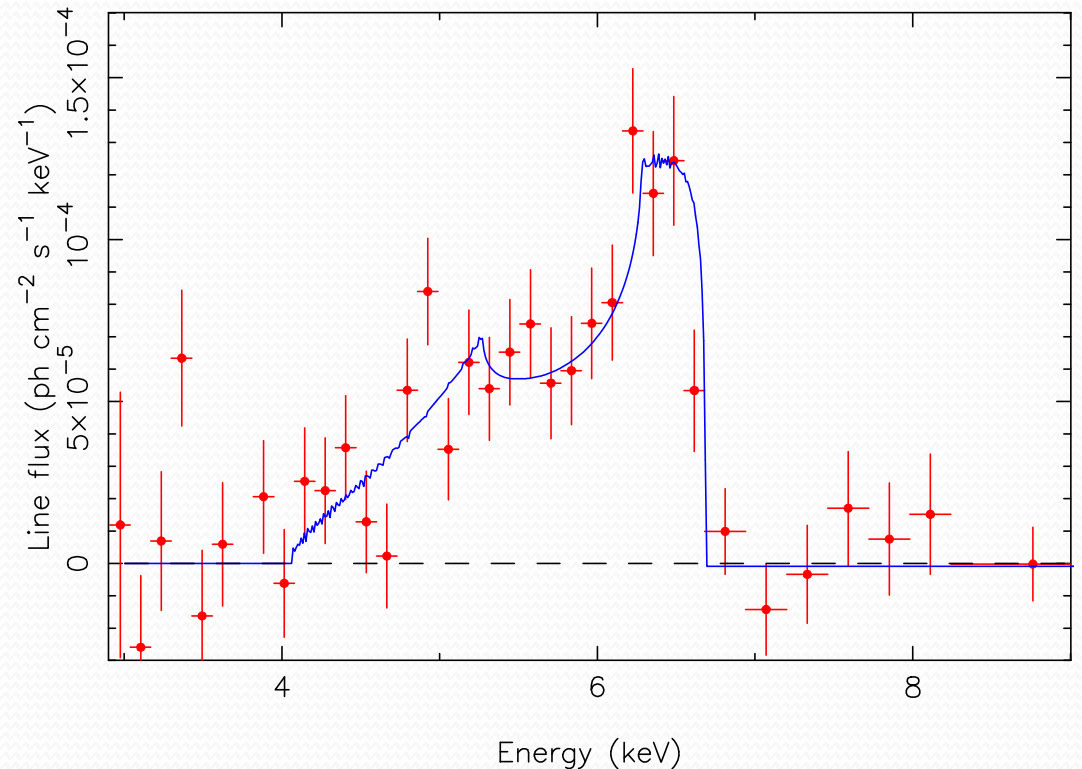




Armitage, P. J., Reynolds, C. S. 2003, *MNRAS*, 341, 1041

# Fe K $\alpha$ spectral line

- broad emission line at 6.4 keV
- asymmetric profile with narrow bright **blue** peak and wide faint **red** peak
- Line width corresponds to velocity:
  - $v \sim 100.000$  km/s (MCG-6-30-15)
  - $v \sim 48.000$  km/s (MCG-5-23-16)
  - $v \sim 20.000 - 30.000$  km/s (other AGN)
- variability of both: line shape and intensity
- Importance:
  1. Studying accretion disk emission close to SMBH
  2. probing strong gravity effects and testing GR predictions
  3. determining SMBH properties

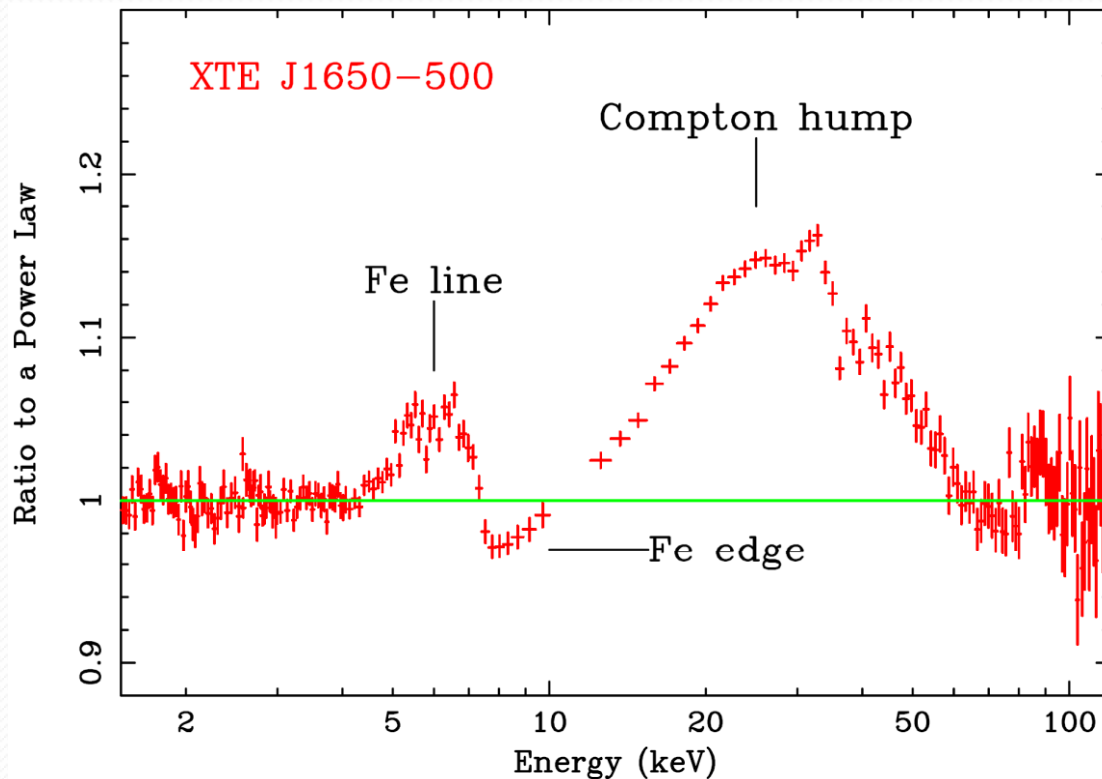


The Fe K $\alpha$  line profile from Seyfert I galaxy MCG-6-30-15 observed by the ASCA (Tanaka, Y. et al, 1995, *Nature*, **375**, 659) and the modeled profile expected from an accretion disk around a Schwarzschild BH.

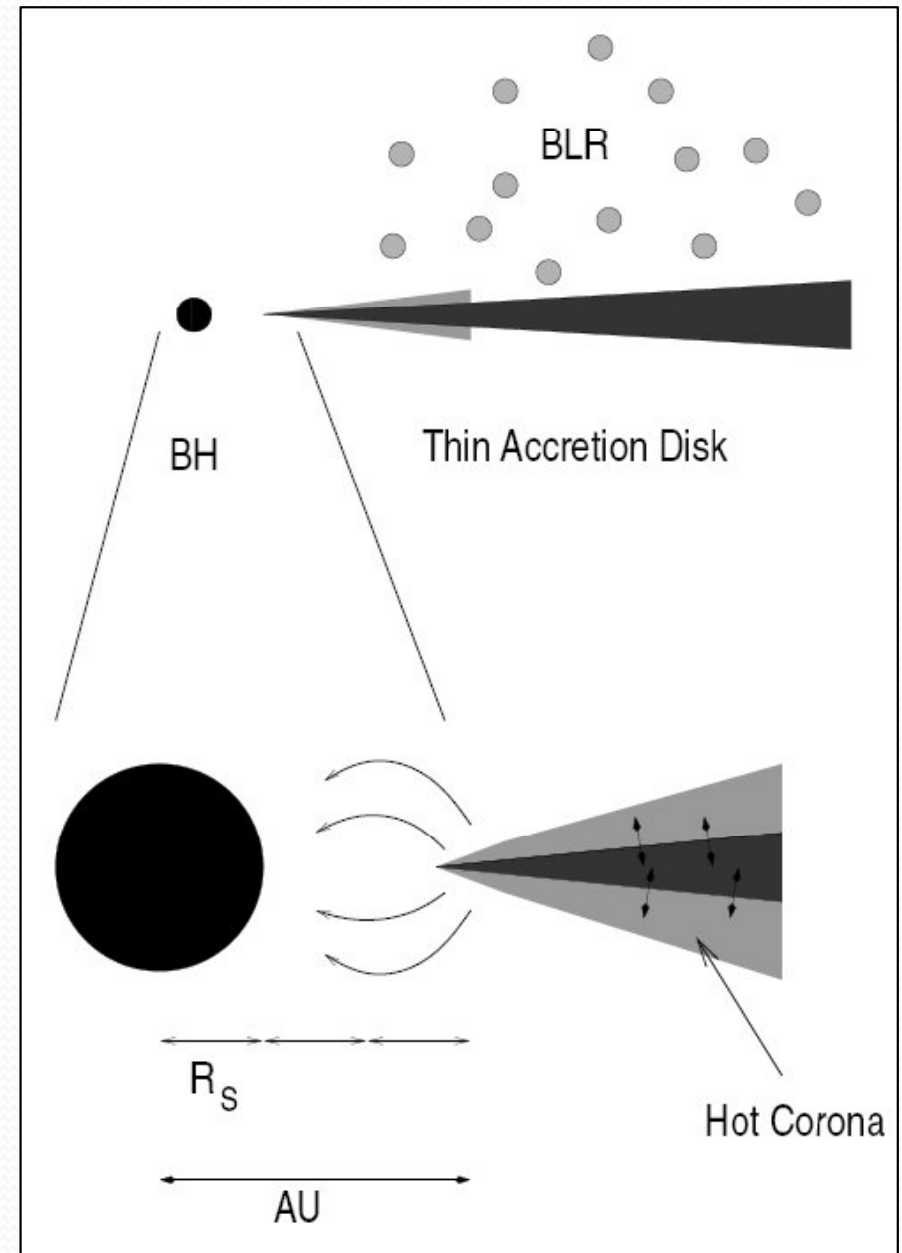


# Production of Fe $K\alpha$ : thin disk + hot corona

- Hard X-ray (power-law) continuum illuminates accretion disk
- Photoelectric absorption of hard X-ray photons followed by fluorescent line emission at 6.4 keV
- Compton reflection hump at 30 keV



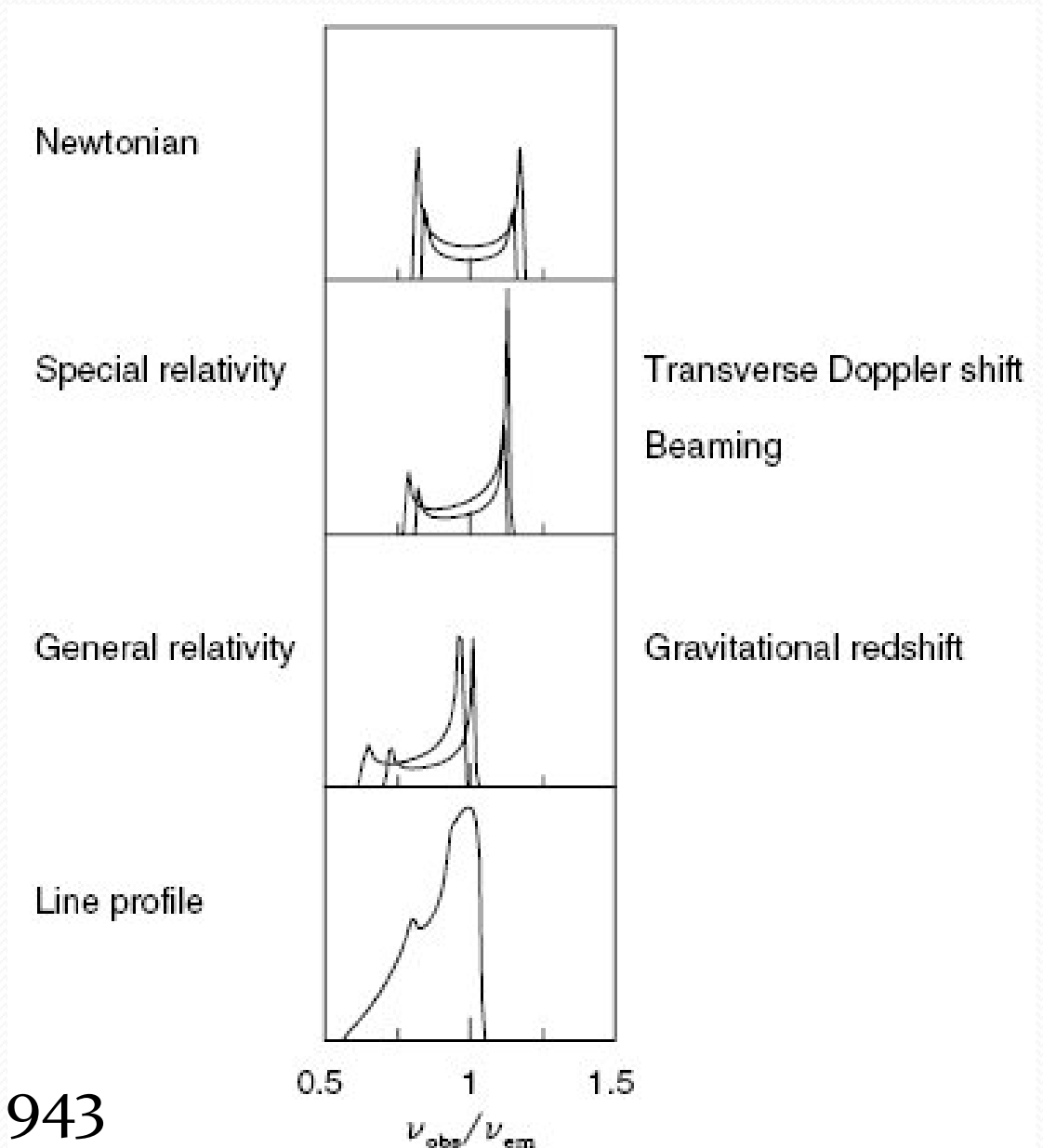
Fabian, A. C. 2006, *AN*, 327, 943



Wilms et al. 2004, *MemSAI*, 75, 519

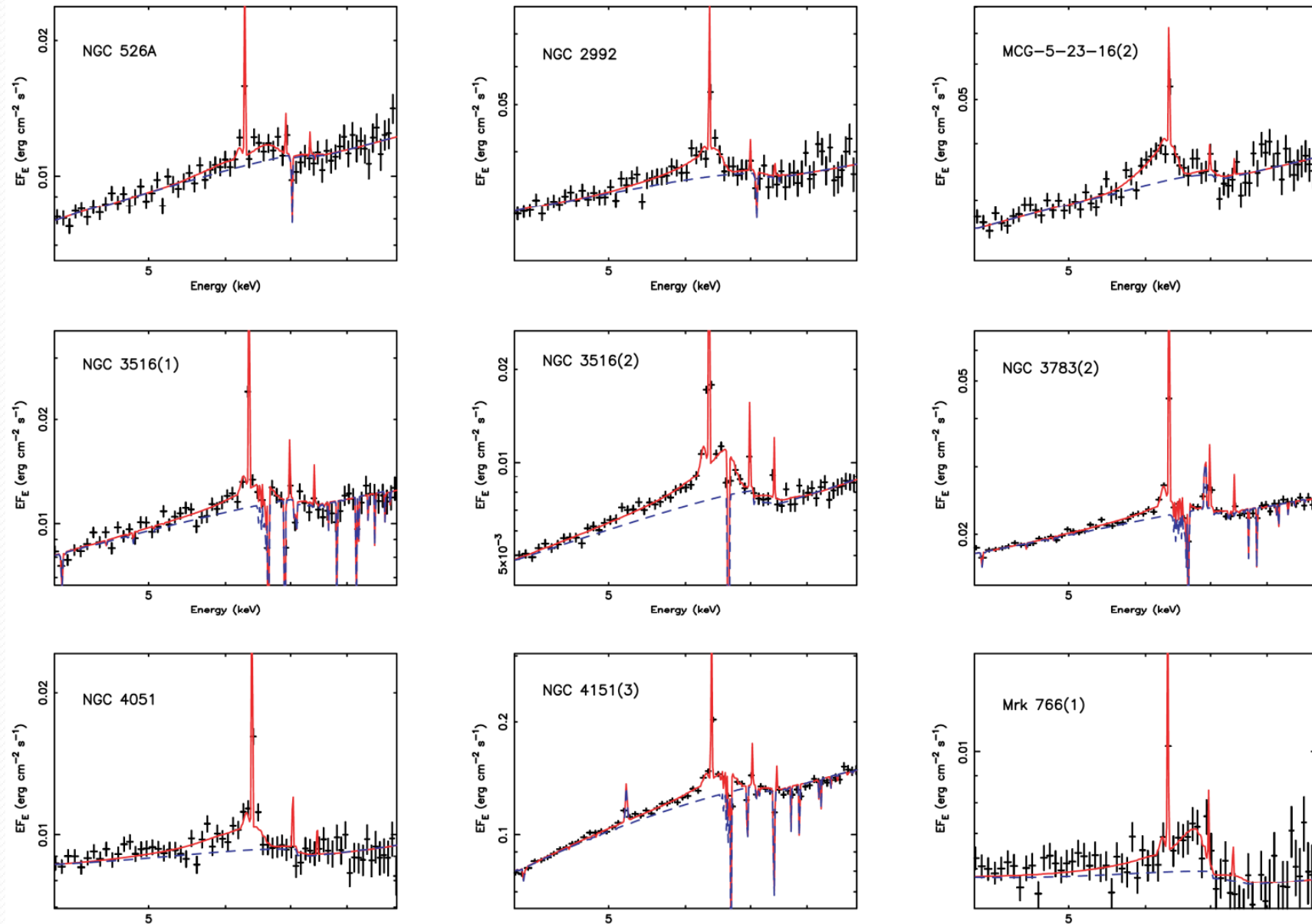
# Relativistic effects on Fe K $\alpha$ line

- Doppler shift: symmetric, double-peaked profile
- Relativistic beaming: enhance blue peak relative to red peak
- Gravitational redshift: smearing blue emission into red



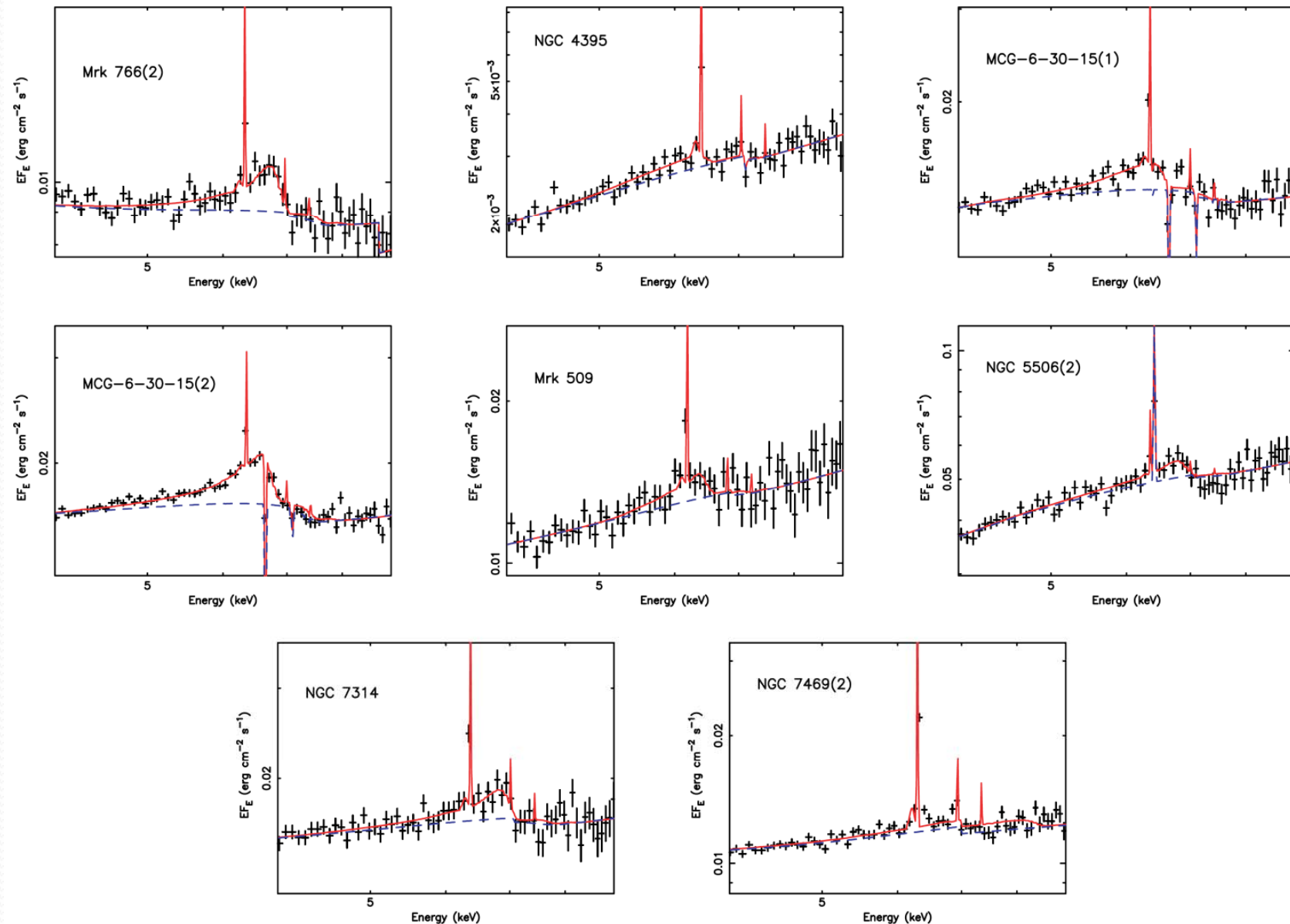
Fabian, A. C. 2006, *AN*, 327, 943

# Some observed Fe K $\alpha$ line profiles I



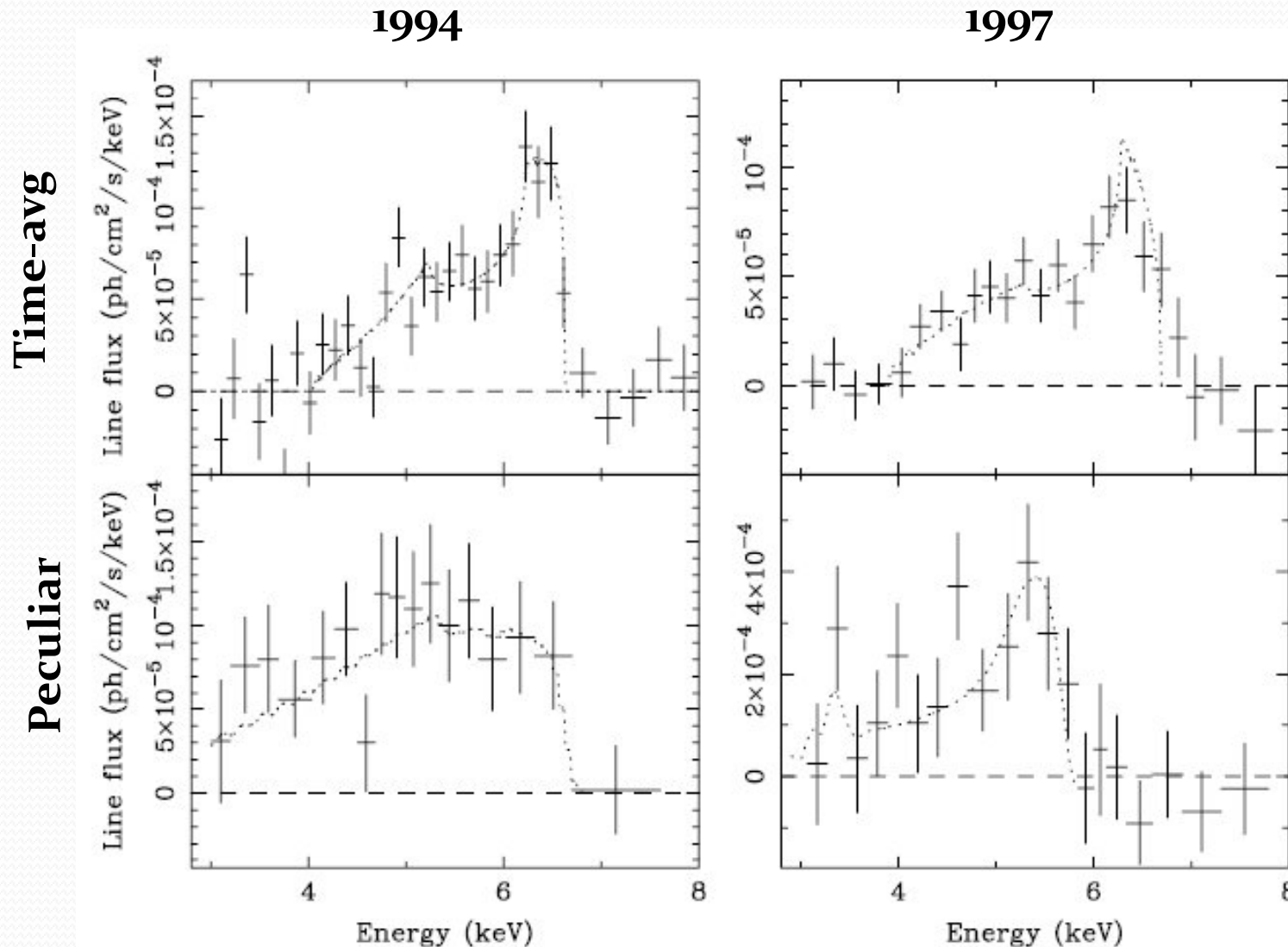
Nandra et al, 2007, *MNRAS*, **382**, 194

# Some observed Fe K $\alpha$ line profiles II



Nandra et al, 2007, *MNRAS*, **382**, 194

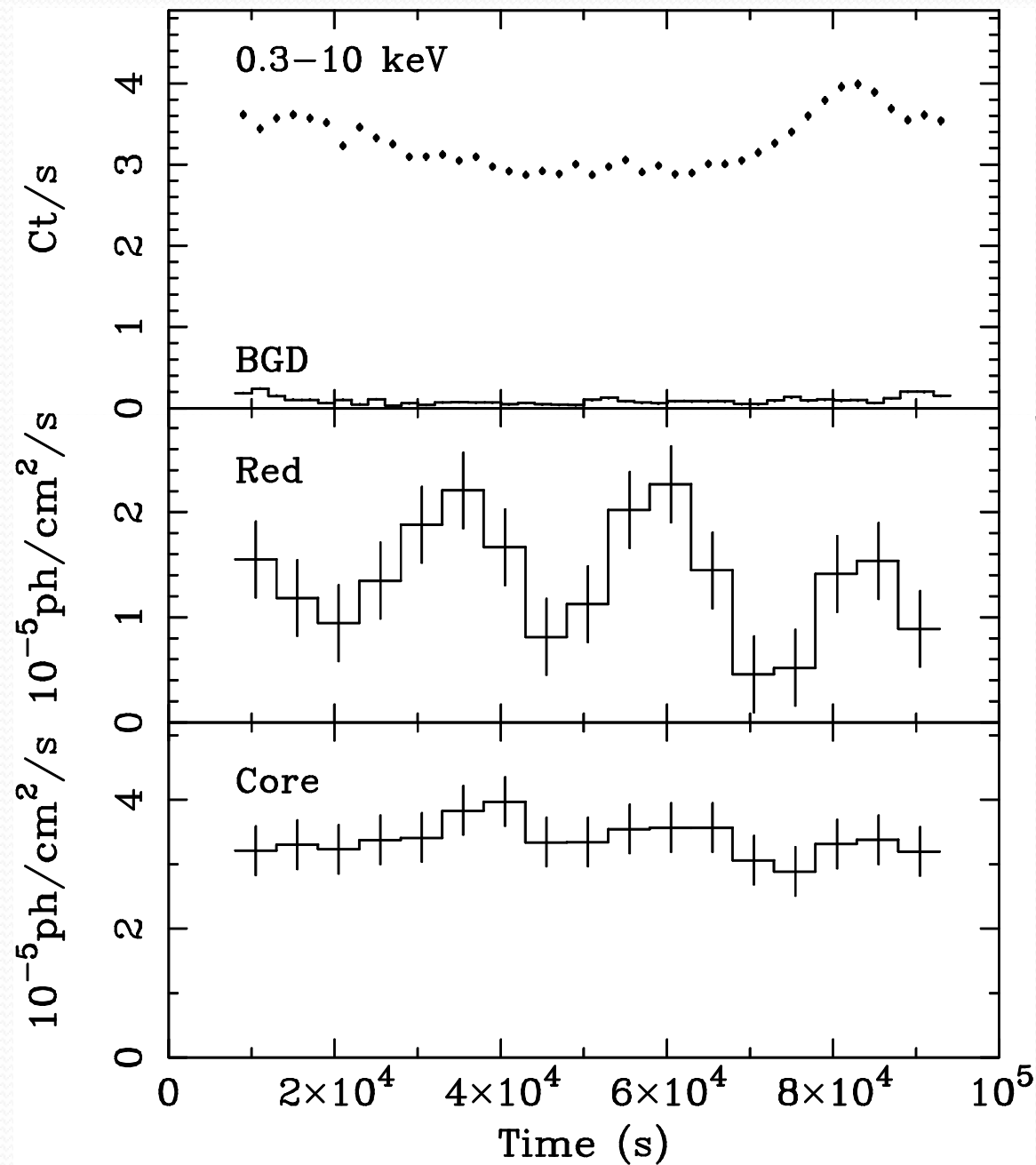
# Observed variability of the Fe K $\alpha$ line shape: MCG-6-30-15



- Both peculiar line shapes can be explained by large gravitational redshift in small radii on the accretion disk

Reynolds, C. S.,  
Nowak, M. A.  
2003, *Physics Reports*, 377, 389

# Observed light curves of the Fe K $\alpha$ line



The light curves of the 0.3-10 keV flux of NGC 3516 (top), the Fe K $\alpha$  5.8-6.2 keV "red" feature (middle), and the 6.4 keV line core (bottom), observed by XMM-Newton

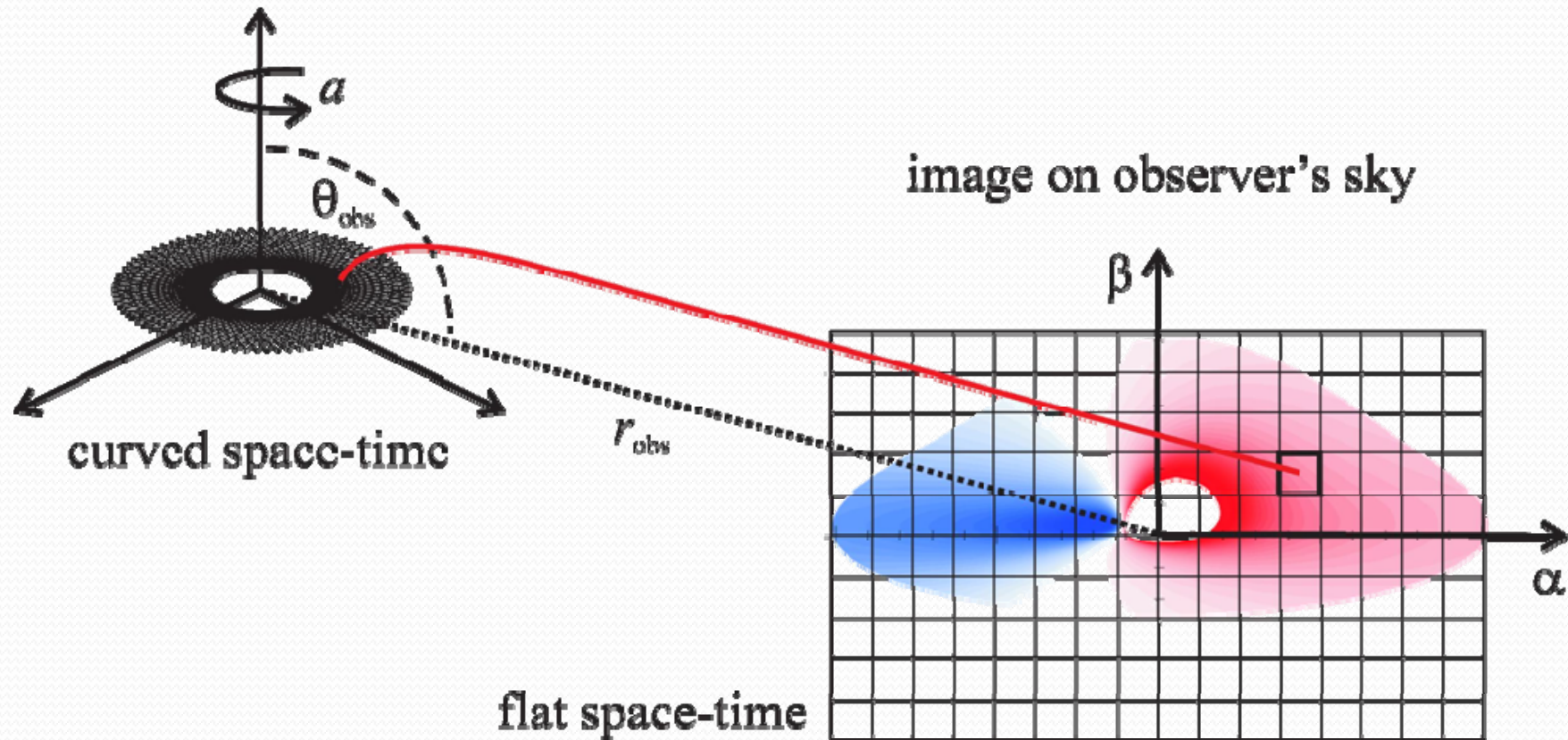
Iwasawa, Miniutti & Fabian, 2004, *MNRAS*, **355**, 1073

# Our investigations and results

1. Modeling of emission of an accretion disk around a SMBH using numerical simulations based on a ray-tracing method in Kerr metric (first results obtained in 2001.)
2. Investigation of the effects of strong gravitational field around a SMBH
3. Studying the variability of Fe  $K\alpha$  line due to:
  - i. internal causes:
    - disk instability and perturbations of its emissivity
  - ii. external causes:
    - absorption by X-ray absorbers
    - gravitational microlensing

**Overview:** Jovanović P., Popović L. Č., 2009, chapter in book “*Black Holes and Galaxy Formation*”, Nova Science Publishers Inc, Hauppauge NY, USA, 249-294 (arXiv:0903.0978)

# Ray-tracing in Kerr metric

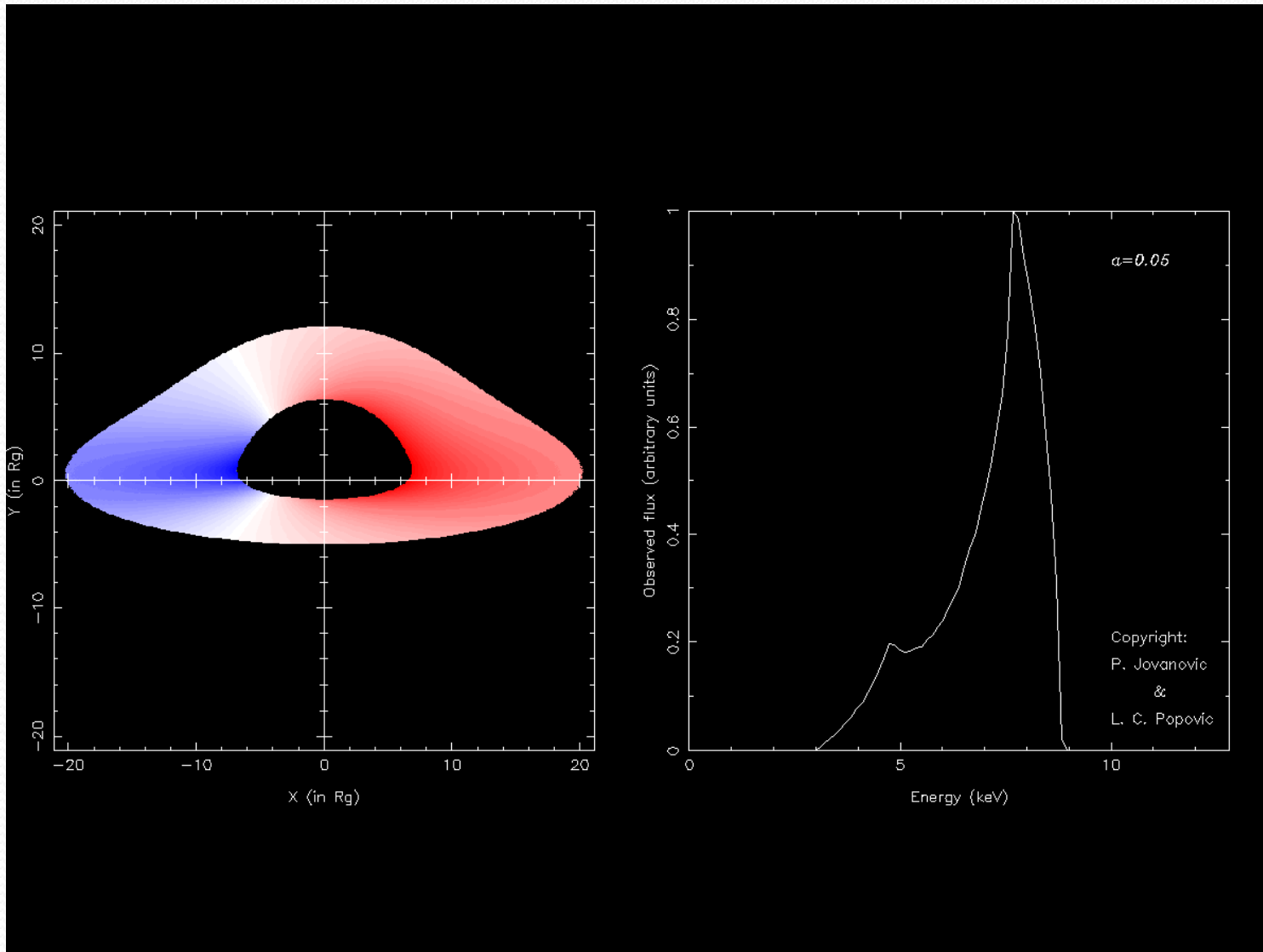


- Surface emissivity of the disk:  $\varepsilon(r) = \varepsilon_0 \cdot r^q$

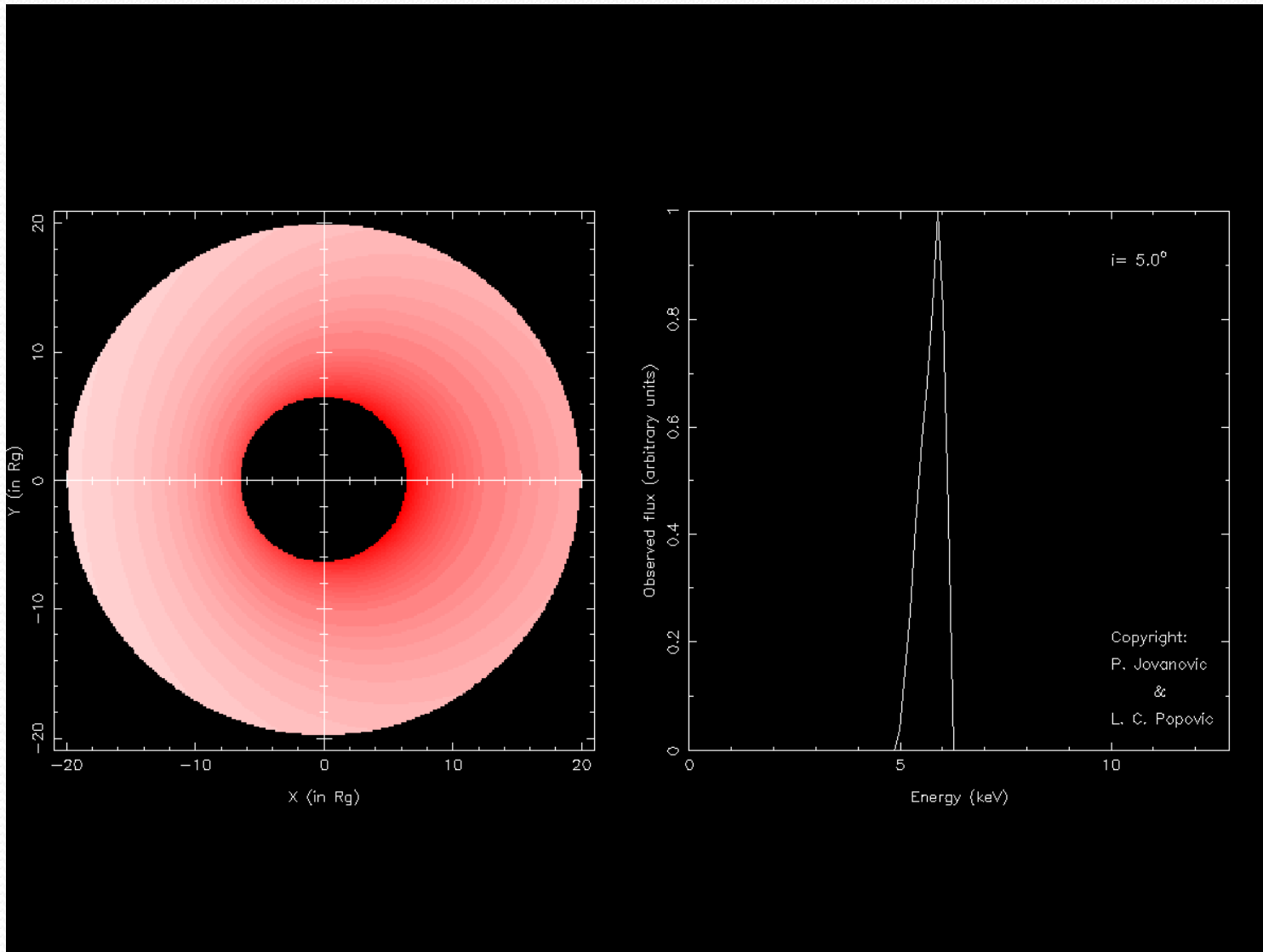
- Total observed flux:  $F_{obs}(E_{obs}) = \int_{image} \varepsilon(r) \cdot g^4 \delta(E_{obs} - gE_0) d\Xi, \quad g = \frac{V_{obs}}{V_{em}}$



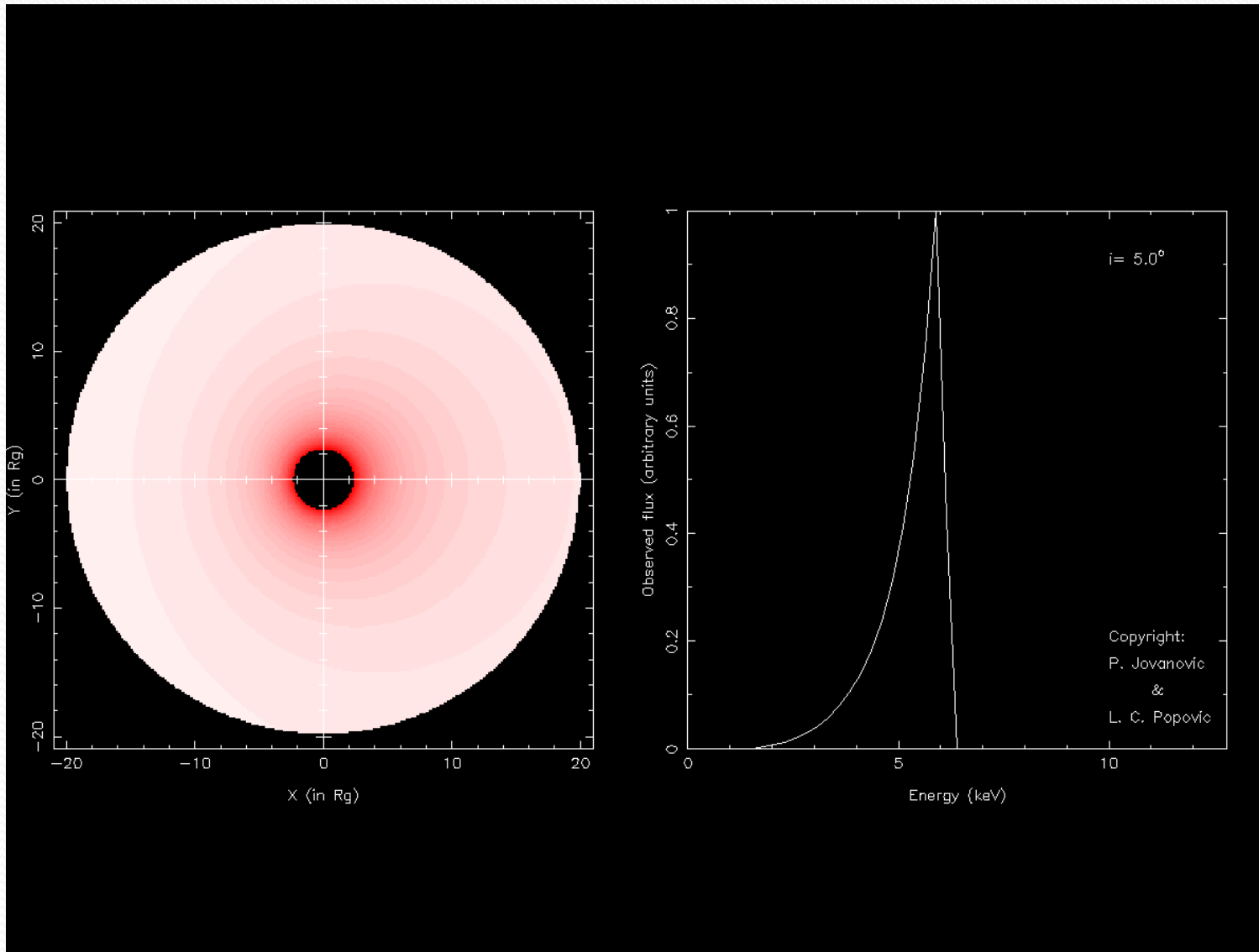
Numerical simulations of a highly inclined accretion disk ( $i=75^\circ$ ) for different values of angular momentum parameter  $a$  (left) and the corresponding profiles of the Fe  $K\alpha$  line (right)

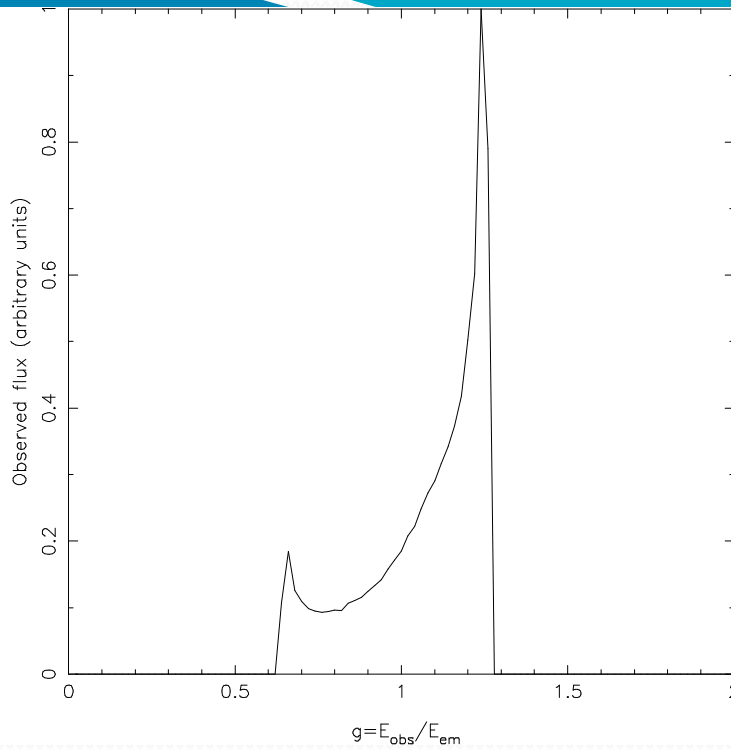
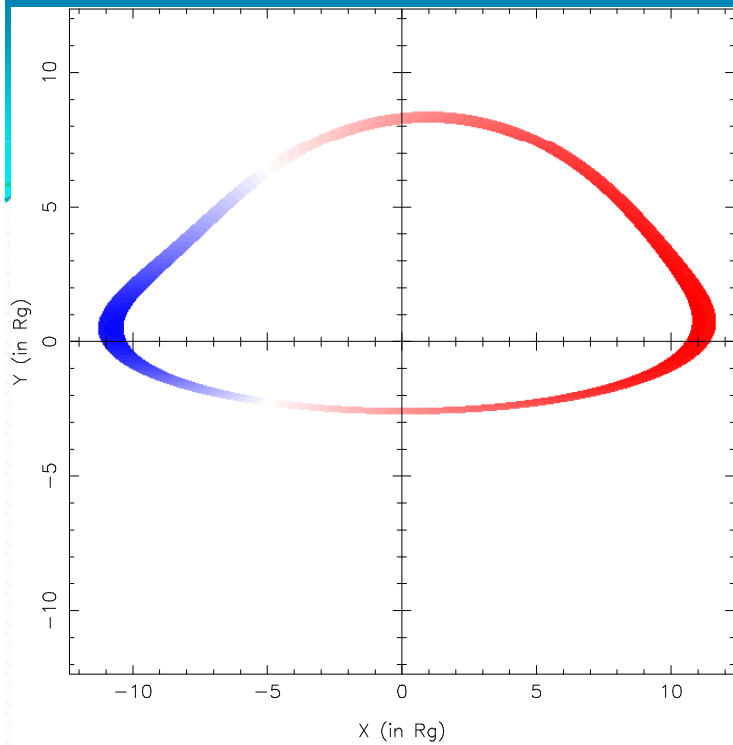


Numerical simulations of an accretion disk in Schwarzschild metric for different inclination angles  $i$  (left) and the corresponding profiles of the Fe  $K\alpha$  line (right)



Numerical simulations of an accretion disk in Kerr metric with angular momentum parameter  $a = 0.998$  for different inclination angles  $i$  (left) and the corresponding profiles of the Fe  $K\alpha$  line (right)

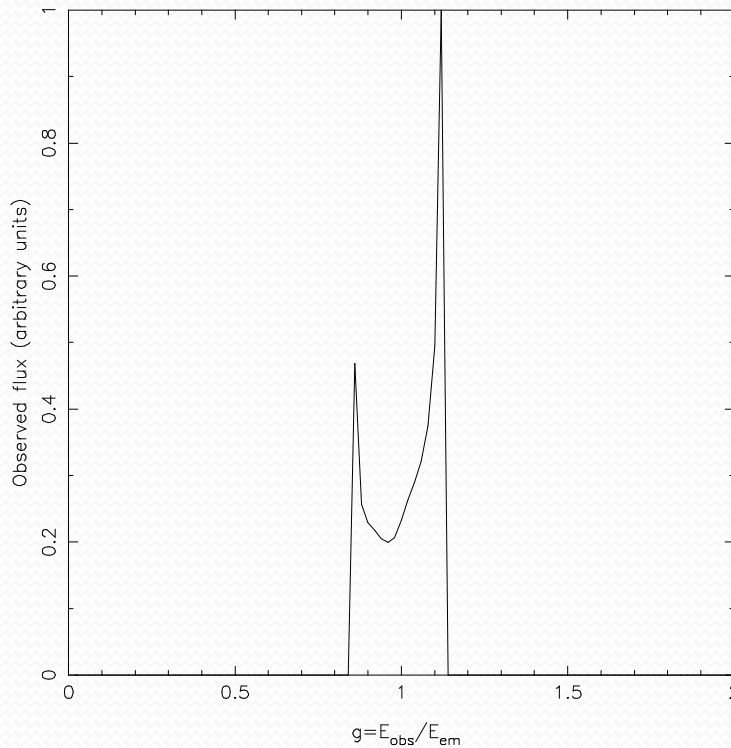
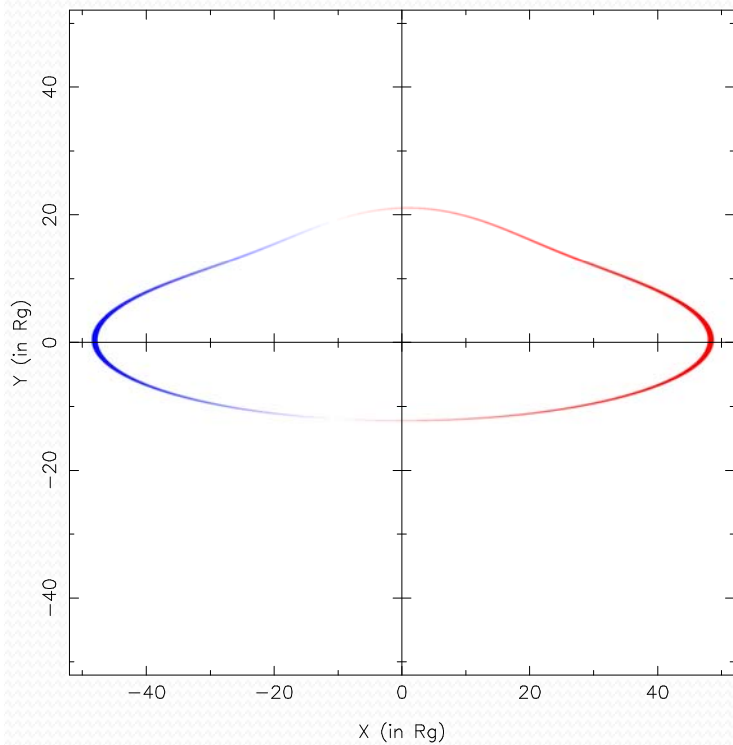




*Left:* illustrations of the Fe K $\alpha$  line emitting region in form of narrow annulus, extending from:

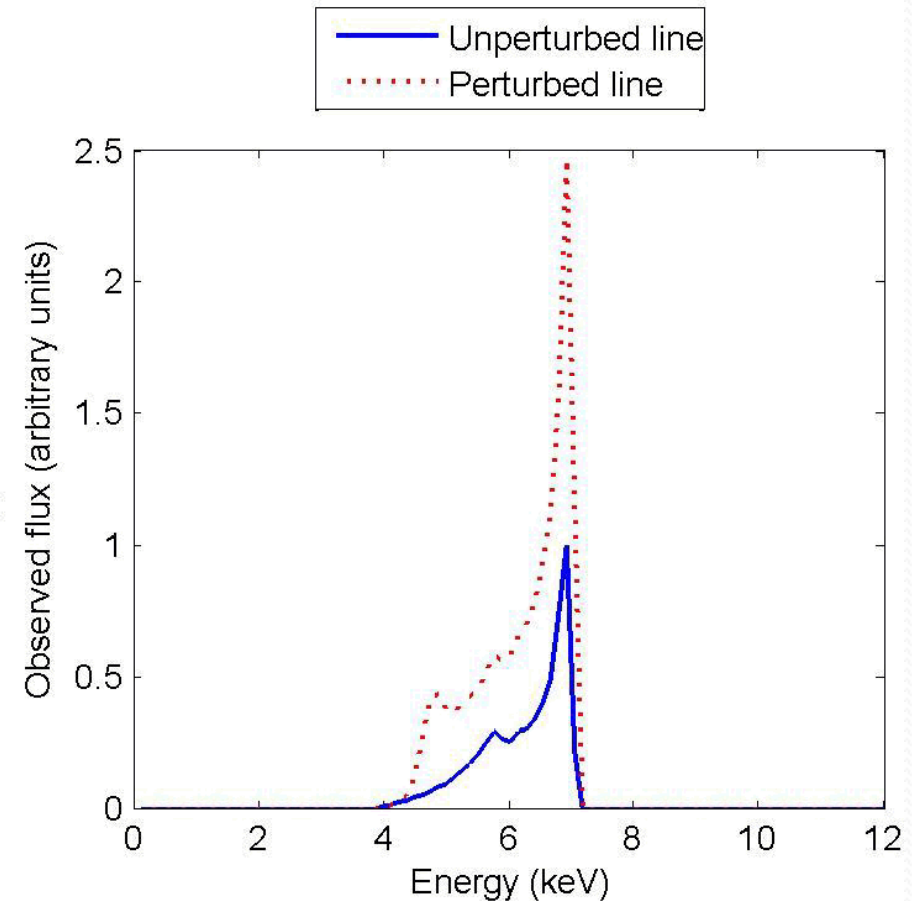
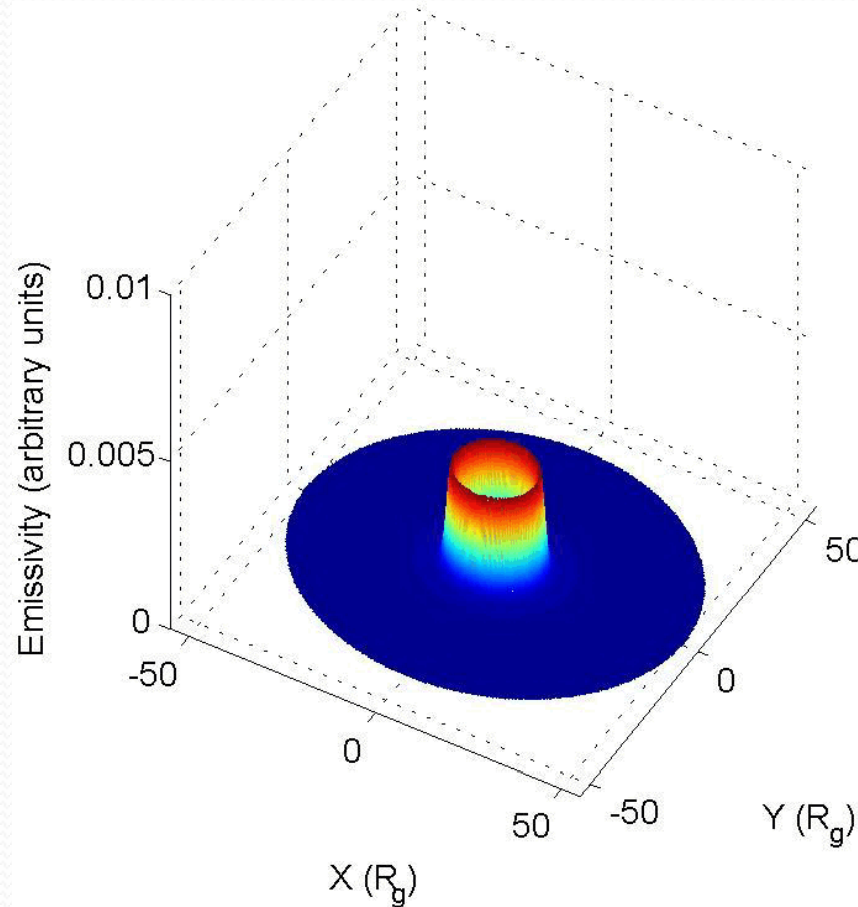
$R_{in} = 10 R_g$  to  $R_{out} = 11 R_g$  (top) and  $R_{in} = 50 R_g$  to  $R_{out} = 51 R_g$  (bottom).

*Right:* the corresponding Fe K $\alpha$  line profiles.



P. Jovanović &  
L. Č. Popović, 2008,  
*Fortschr. Phys.* **56**,  
No. 4 – 5, 456

# Modeled variations of the Fe K $\alpha$ line due to disk emissivity perturbations



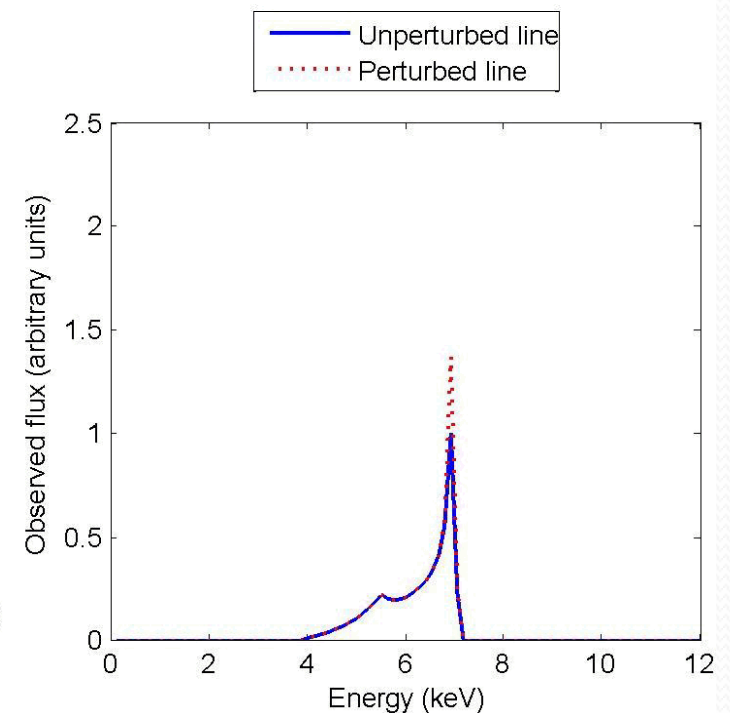
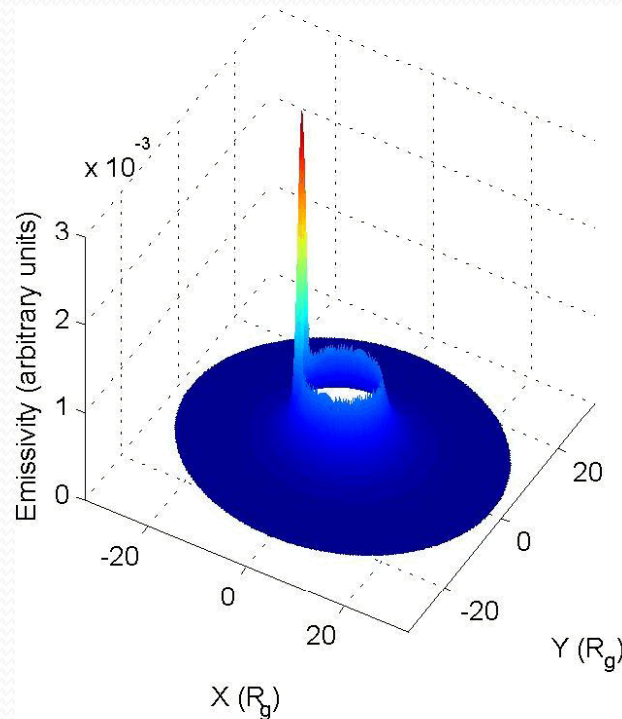
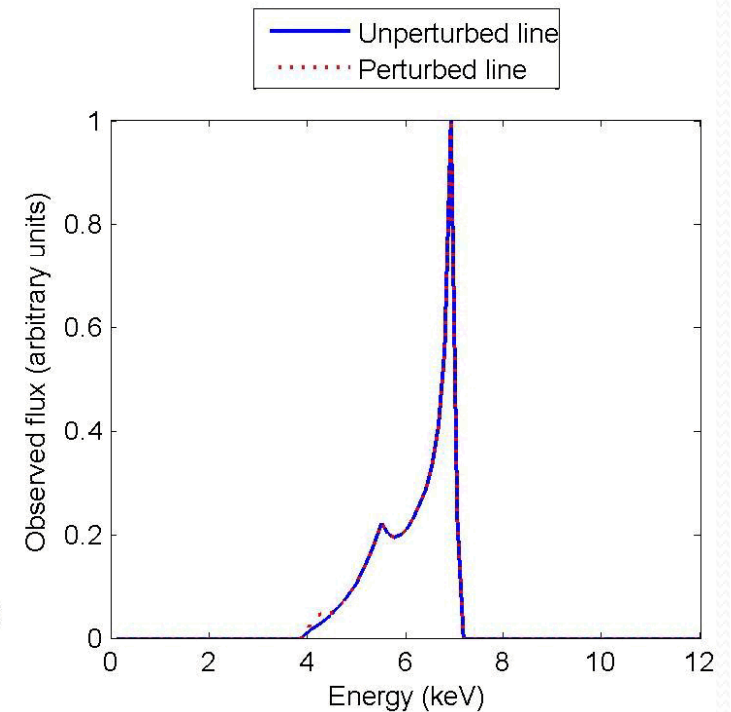
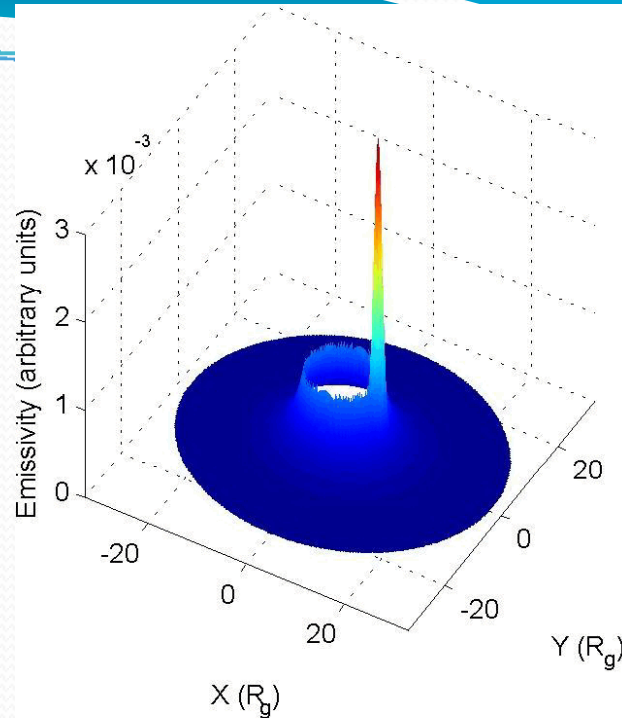
Numerical simulations of disk emissivity perturbations in Schwarzschild metric and the corresponding variations of the Fe K $\alpha$  line profile

$$\varepsilon_1(r) = \varepsilon(r) \cdot \left( 1 + \varepsilon_p \cdot e^{-\left(\frac{r-r_p}{w_p}\right)^2} \right)$$

Numerical simulations of emissivity perturbations along the receding (top) and approaching (bottom) side of the disk in Schwarzschild metric and the corresponding variations of the Fe K $\alpha$  line profile

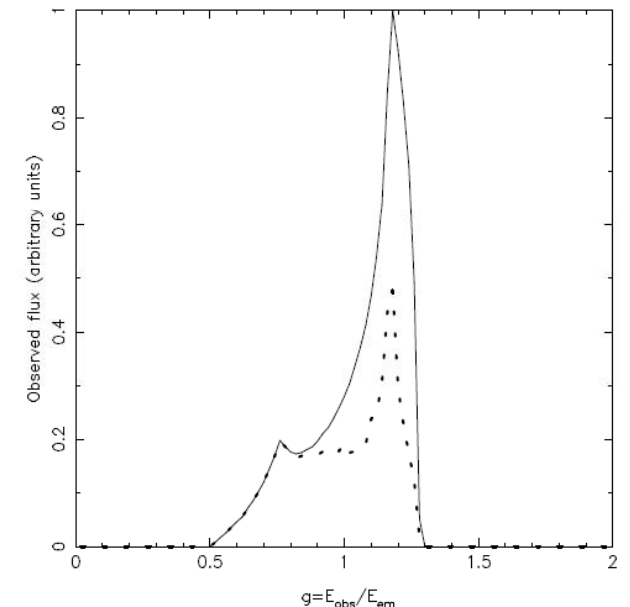
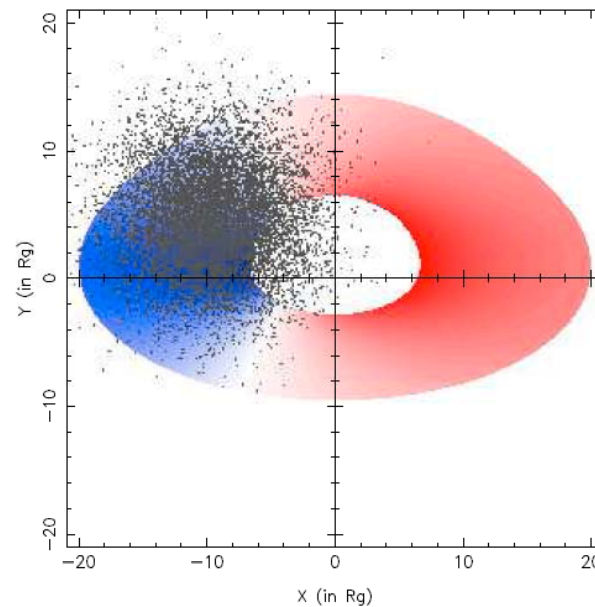
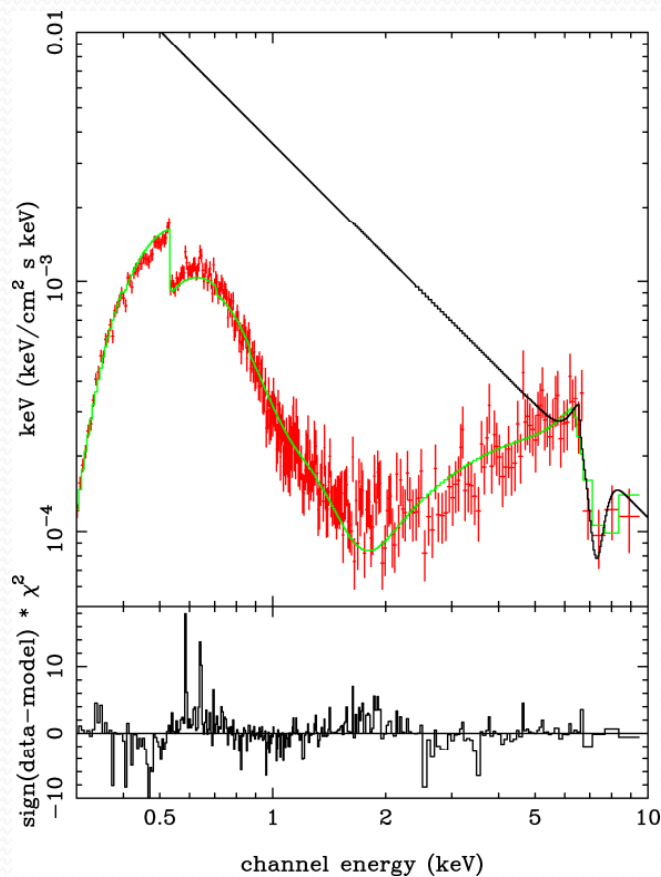
$$\varepsilon_2(x_p, y_p) = \varepsilon(r(x_p, y_p)) \cdot \left( 1 + \varepsilon_p \cdot e^{-\left( \left( \frac{x-x_p}{w_x} \right)^2 + \left( \frac{y-y_p}{w_y} \right)^2 \right)} \right)$$

Jovanović, P., Popović, L. Č., Stalevski, M., Shapovalova, A. I. 2010. *ApJ*, 718, 168

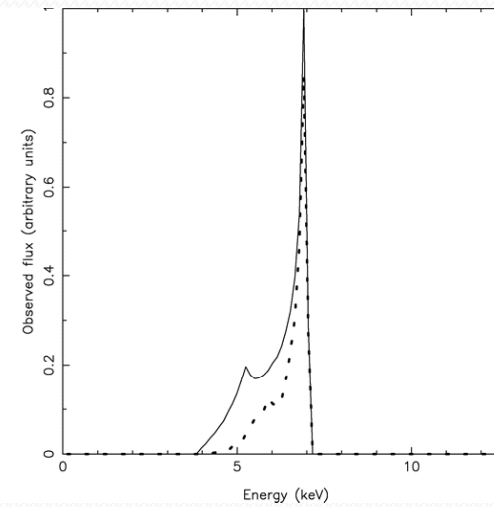
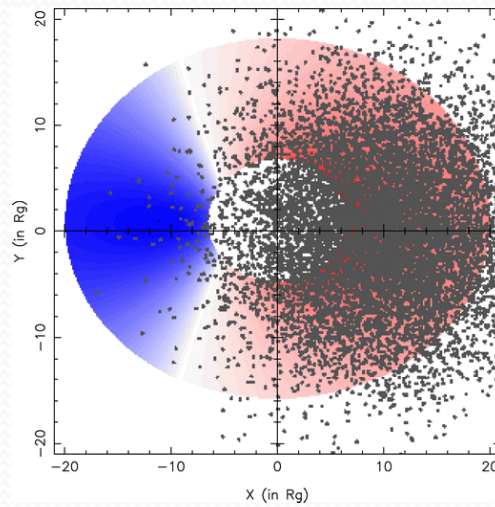
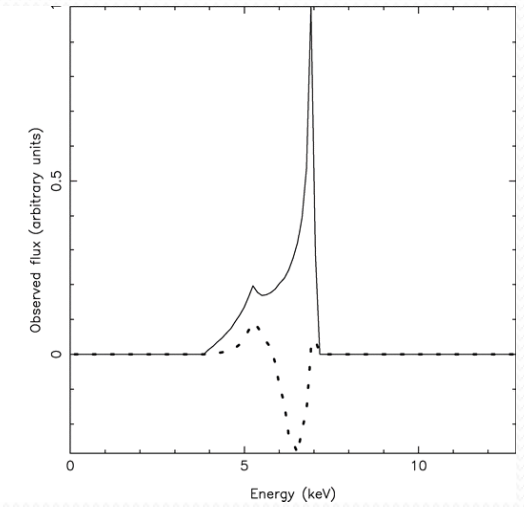
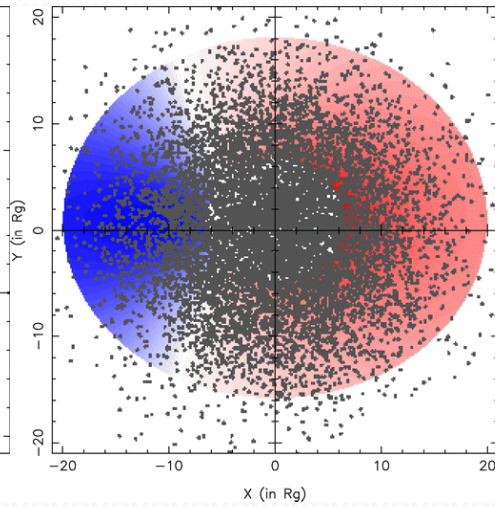
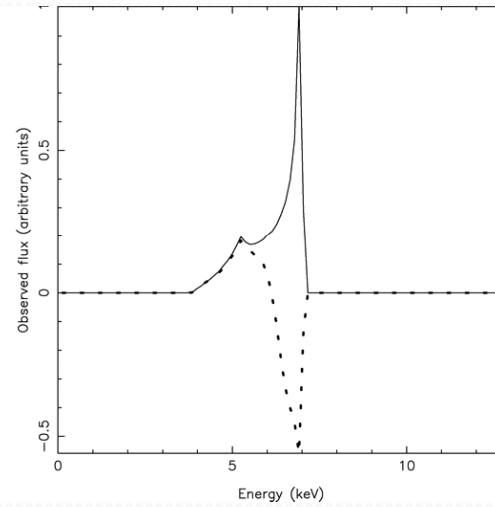
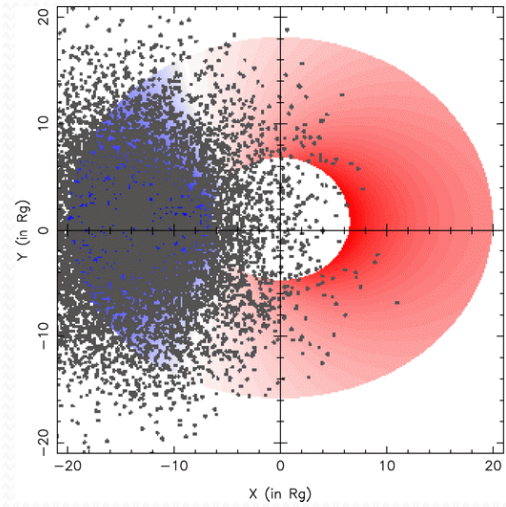


# A model of X-ray absorption region

- composed from a large number of small spherical absorbing clouds which have normal distribution



- Done et al. 2007, MNRAS, 374, L15: sharp feature at  $\sim 7$  keV results from absorption/scattering/emission of iron  $K\alpha$  lines in the wind and can be fitted by P Cygni profile

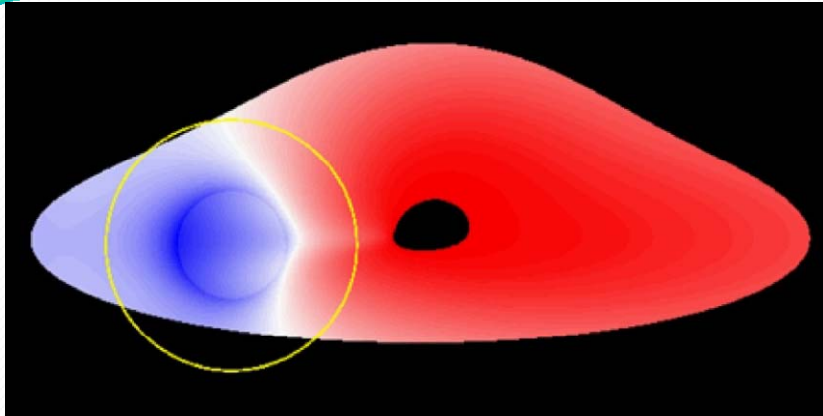


Jovanović, P., Popović, L. Č., Simić, S. 2009, *NARev*, 53, 156



# Gravitational microlensing

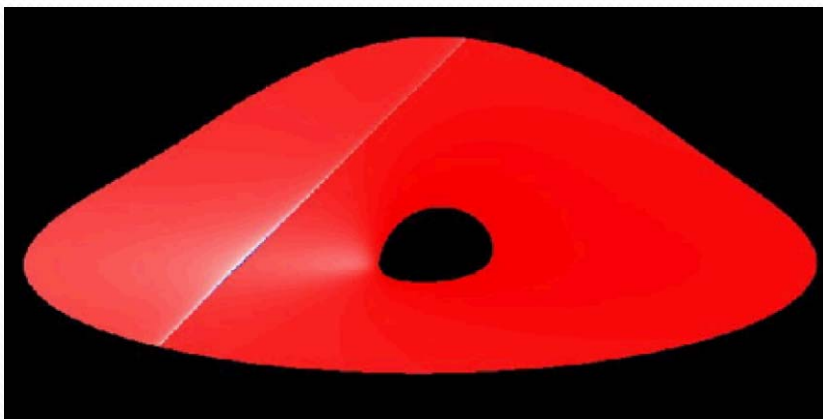
## Point-like



$$A(X, Y) = \frac{u^2(X, Y) + 2}{u(X, Y)\sqrt{u^2(X, Y) + 4}}$$

$$u(X, Y) = \frac{\sqrt{(X - X_0)^2 + (Y - Y_0)^2}}{\eta_0}$$

## • Straight-fold caustic

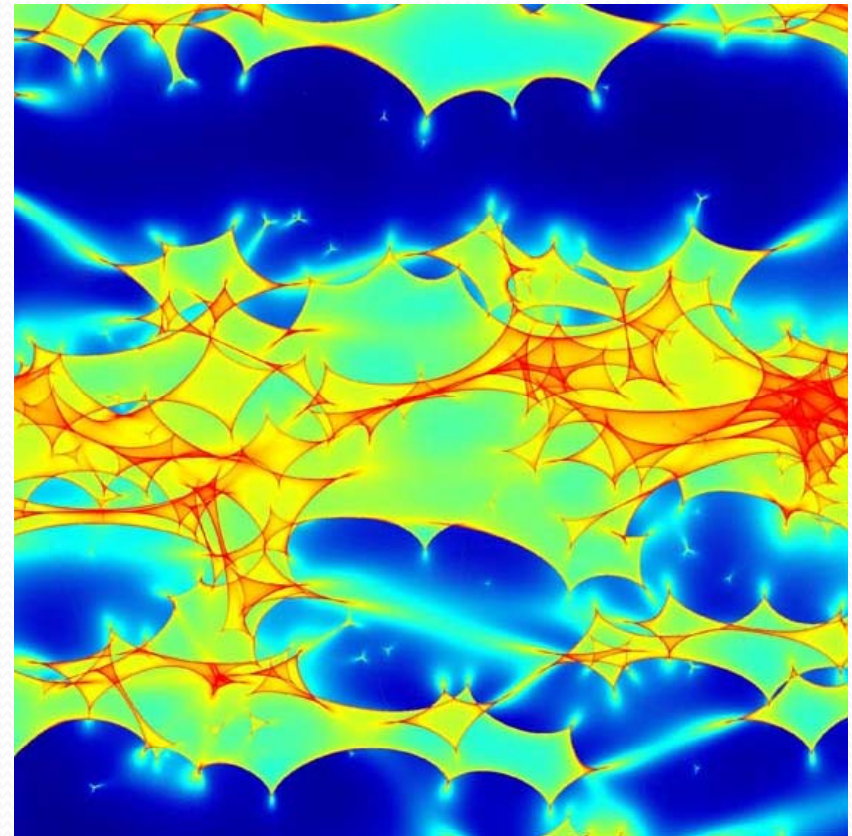


$$A(X, Y) = A_0 + \frac{K}{\sqrt{\kappa(\xi - \xi_c)}} \cdot H(\kappa(\xi - \xi_c))$$

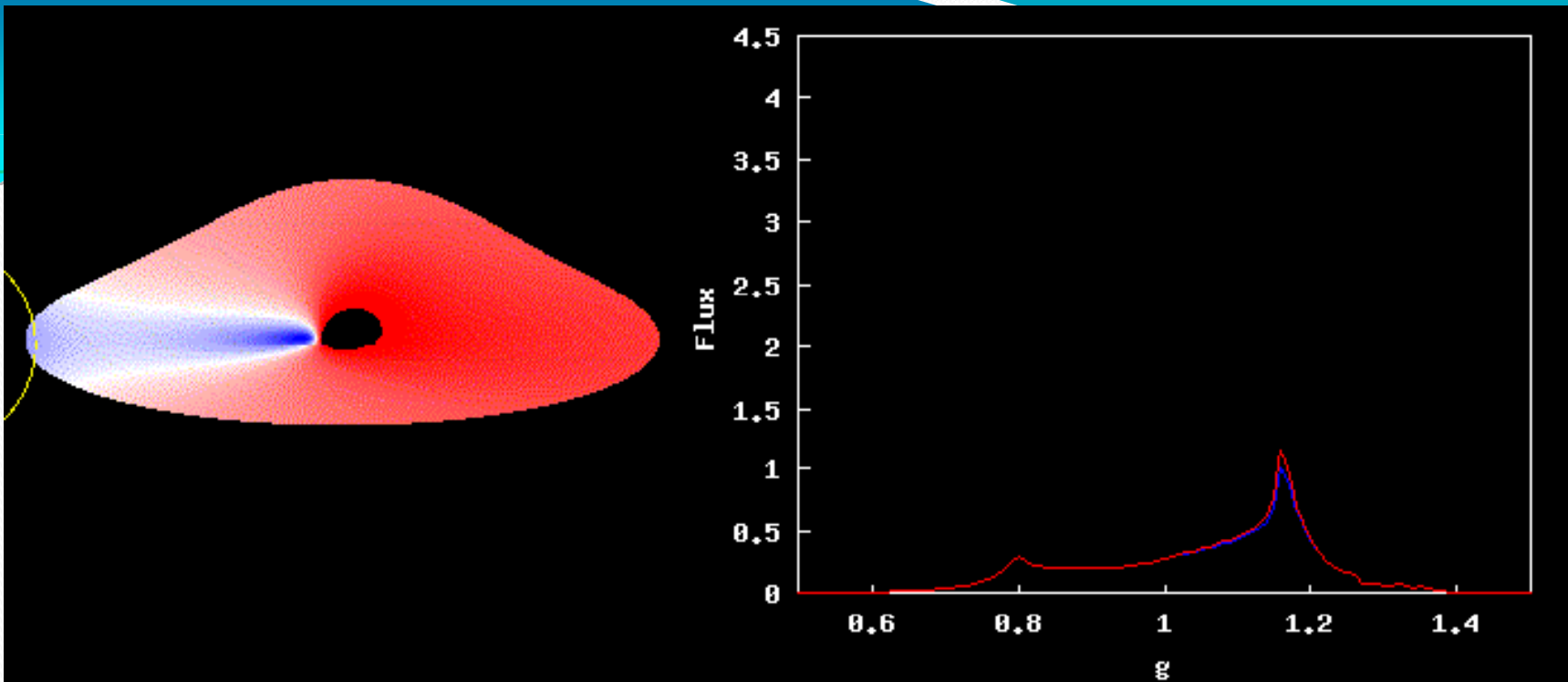
$$K = A_0\beta\sqrt{\eta_0}$$

## • Microlensing magnification map

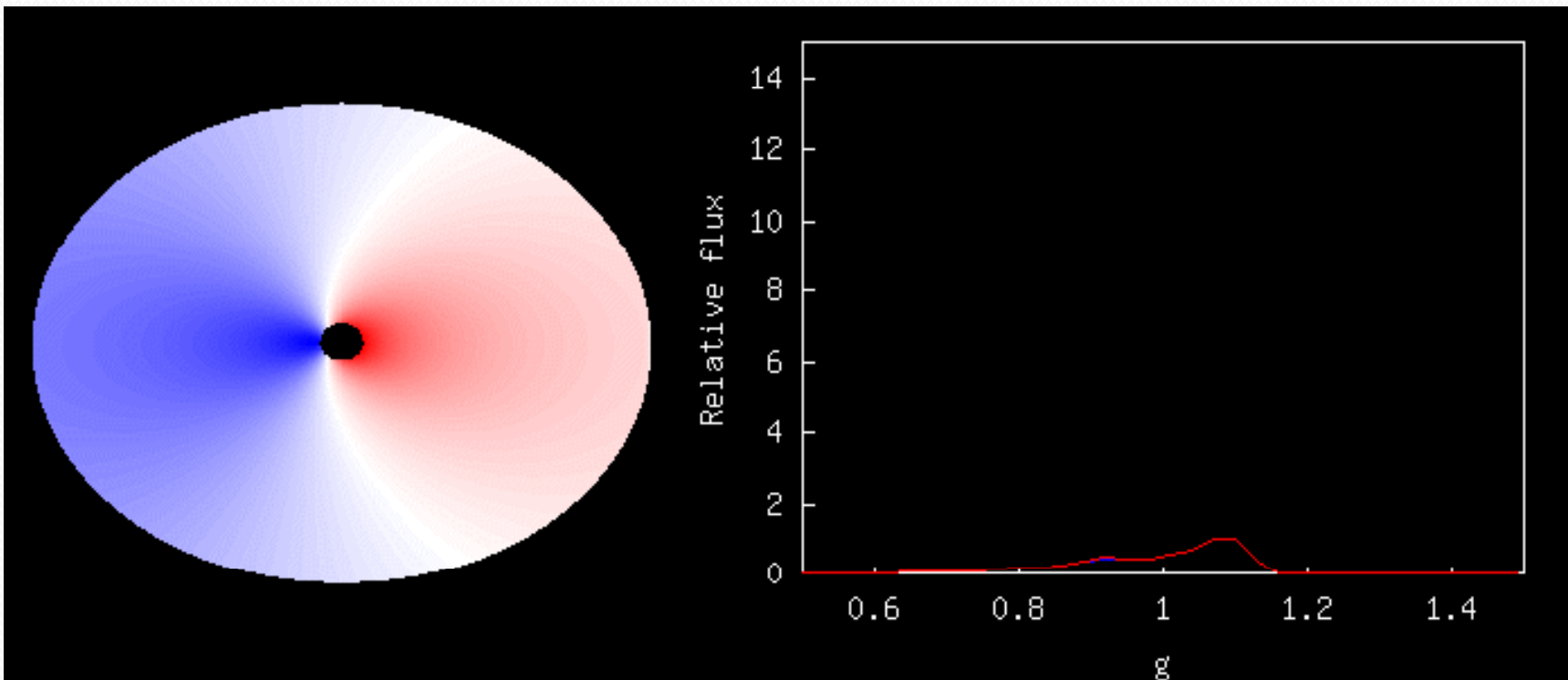
$$\vec{y}(\vec{x}) = \vec{x} - \sum_{i=1}^N m_i \frac{\vec{x} - \vec{x}_i}{|\vec{x} - \vec{x}_i|^2} - \begin{bmatrix} k_c + \gamma & 0 \\ 0 & k_c - \gamma \end{bmatrix} \vec{x}$$



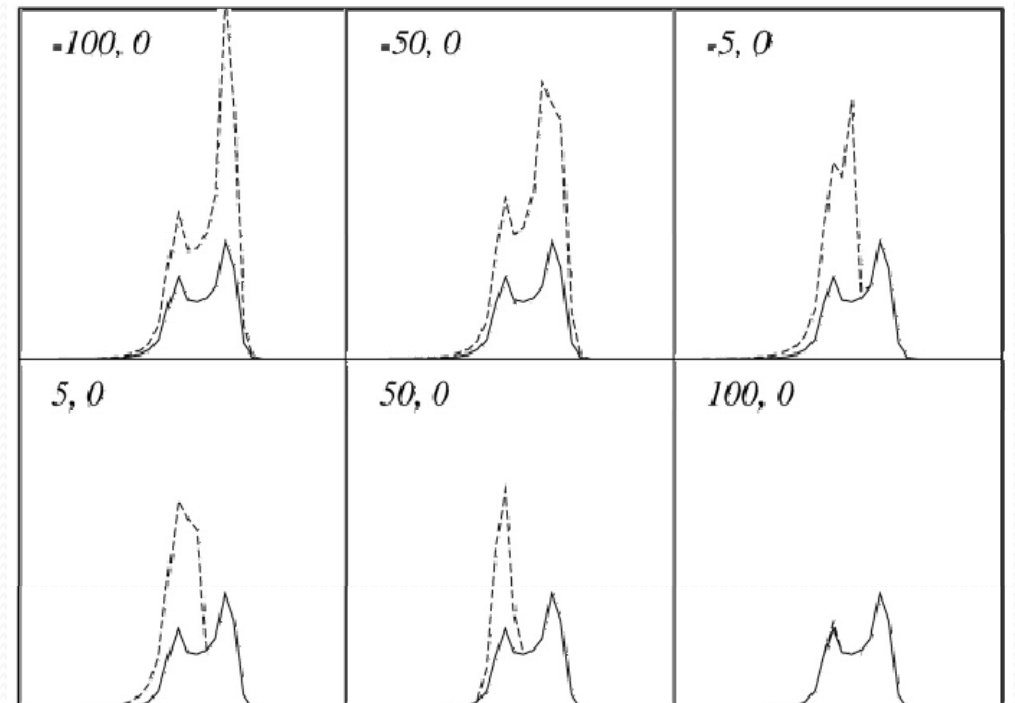
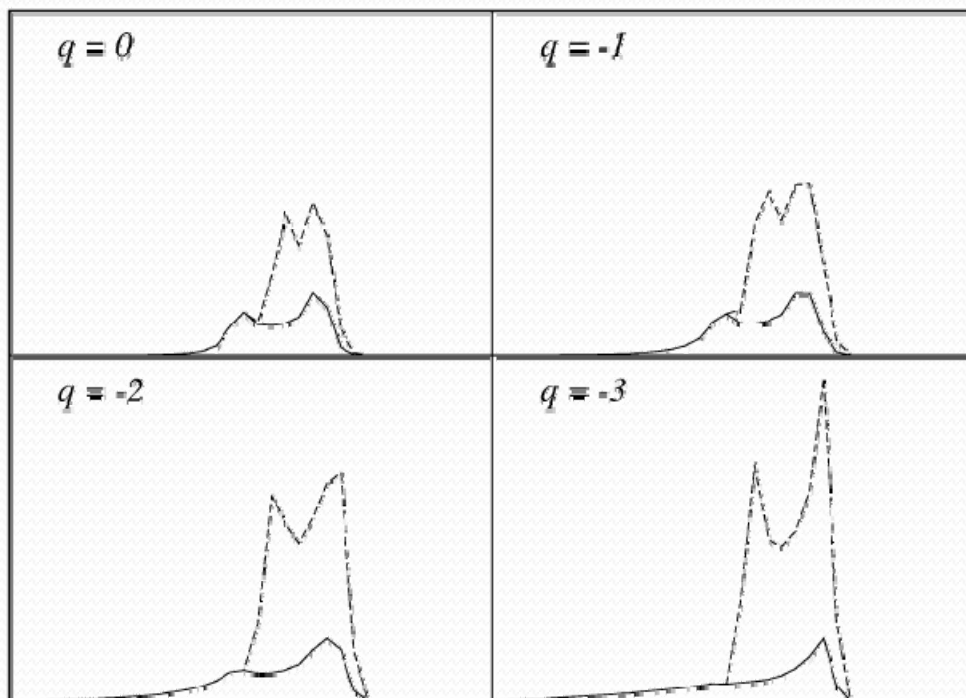
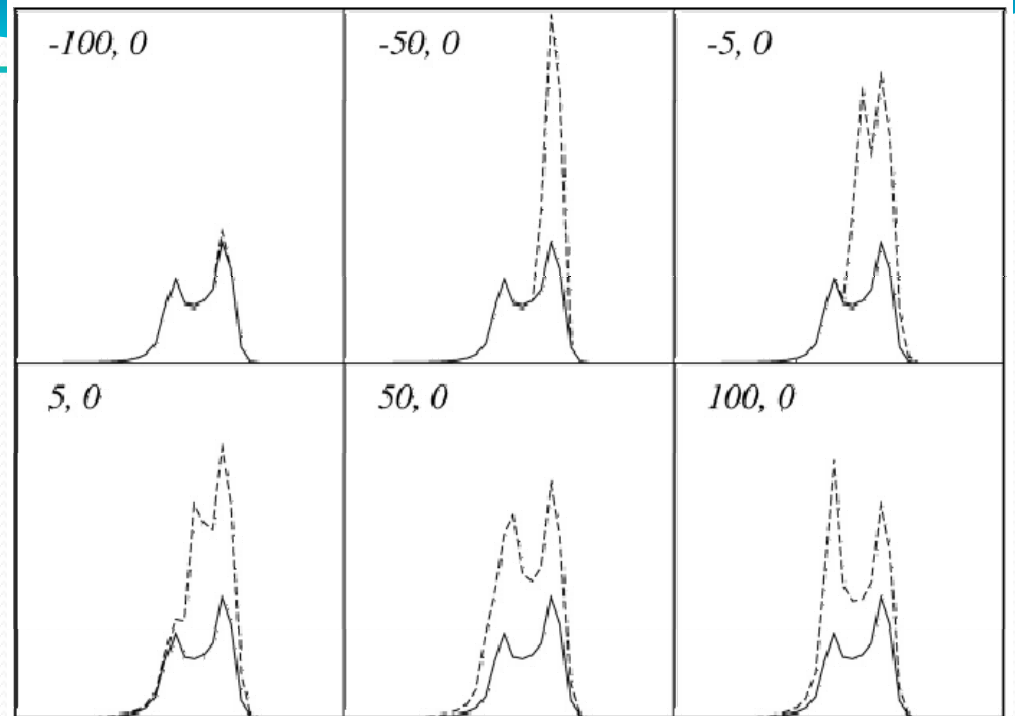
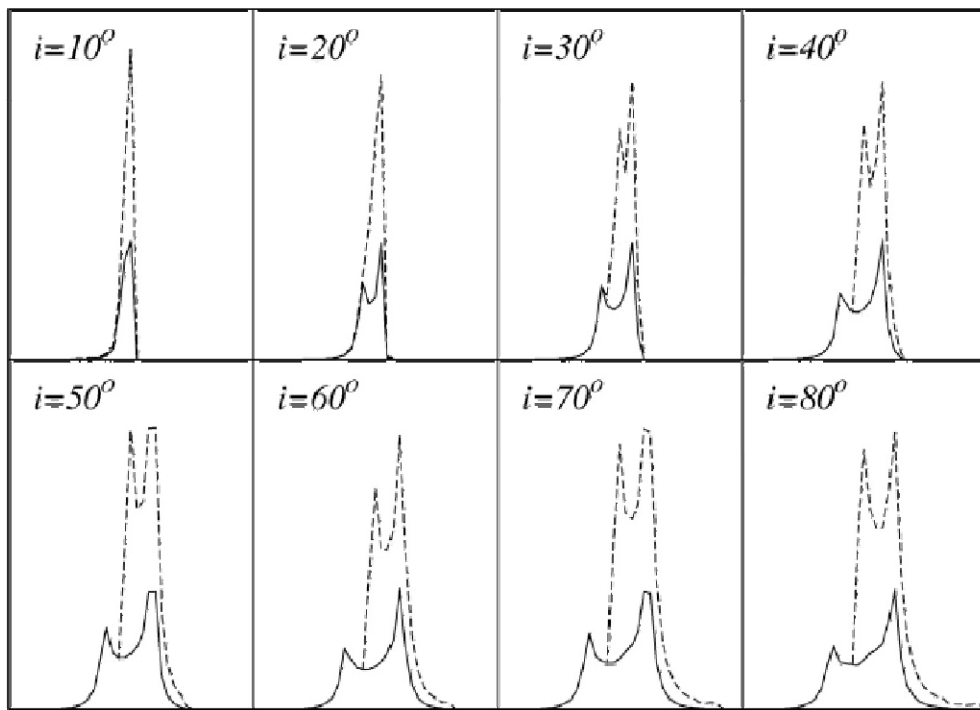
Microlensing magnification map for image A of QSO 2237+0305 ( $k_c = 0.36$ ,  $\gamma = 0.4$ )



Popović, L. Č.,  
 Jovanović, P.,  
 Bon, E.,  
 Dimitrijević, M. :  
 2002, Publ.  
 Astron. Obs.  
 Belgrade, 73, 49



Popović, L. Č.,  
 Jovanović, P.,  
 Mediavilla, E. G.,  
 Muñoz, J. A. 2003.  
*A&AT*, 22, 719



# Conclusions

1. We investigated the Fe  $K\alpha$  line emitted from the innermost parts of accretion disk around SMBH using numerical simulations based on ray-tracing method in Kerr metric
2. The Fe  $K\alpha$  line is useful tool for:
  - studying space-time geometry in vicinity of SMBH
  - determination of black hole properties
  - probing strong gravity effects and test GR predictions
  - studying accretion physics around SMBH

# References

1. Jovanović, P., Popović, L. Č., Stalevski, M., Shapovalova, A. I. 2010. *ApJ*, 718, 168
2. Jovanović, P., Popović, L. Č. 2009. *X-ray Emission From Accretion Disks of AGN: Signatures of Supermassive Black Holes*, chapter in the book "Black Holes and Galaxy Formation", Nova Science Publishers, Inc, Hauppauge NY
3. Jovanović, P., Popović, L. Č., Simić, S. 2009, *NARev*, 53, 156
4. Jovanović, P., Zakharov, A. F., Popović, L. Č., Petrović, T. 2008. *MNRAS*, 386, 397
5. Jovanović, P., Popović, L. Č. 2008. *Fortschritte der Physik*, 56, Issue 4-5, 456
6. P. Jovanović, 2006, *PASP*, 118, 656
7. Popović, L. Č., Jovanović, P., Mediavilla, E. G., Zakharov, A. F., Abajas, C., Muñoz, J. A., Chartas, G. 2006, *ApJ*, 637, 620
8. Popović, L. Č., Jovanović, P., Mediavilla, E. G., Muñoz, J. A. 2003. *A&AT*, 22., Nos. 4-5, 719
9. Popović, L. Č., Mediavilla, E. G., Jovanović, P., Muñoz, J. A. 2003. *A&A*, 398., 975
10. Popović, L. Č., Jovanović, P., Bon, E., Dimitrijević, M. S. 2002. *Publ. Astron. Obs. Belgrade*, 73, 49



Thank you for attention!